

Laser Driven X-ray Radiography On Warm Dense Matter

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WDM: Definition

Warm Dense Matter = Dense plasmas at temperatures of 0.5 – 50 eV
($\approx 5.000 - 500.000$ K) at **around solid density**

WDM \rightarrow **strongly correlated** $\langle E_{pot} \rangle \approx k_B T_e$

WDM \rightarrow **partly degenerated** $k_B T_e \approx E_{Fermi}$

Example:

Titanium @ solid density, $T = 10$ eV:

Coupling parameter: $\Gamma := \frac{\langle E_{pot} \rangle}{k_B T_e} \approx 10$ ($\Gamma \ll 1$ for ideal plasma)

Degeneracy parameter: $\Theta := \frac{k_B T_e}{E_{Fermi}} \approx 2$ ($\Theta \gg 1$ for classical plasma)

Pressure: $p = 5$ MBar (!)

Part of HED: pressures > 1 MBar, energy densities of > 100 J/mm³

WDM: Why Should We Care?

WDM can be found:

- in the center of giant planets or brown dwarfs
- whenever a solid is transformed into a plasma
- during the process of ICF

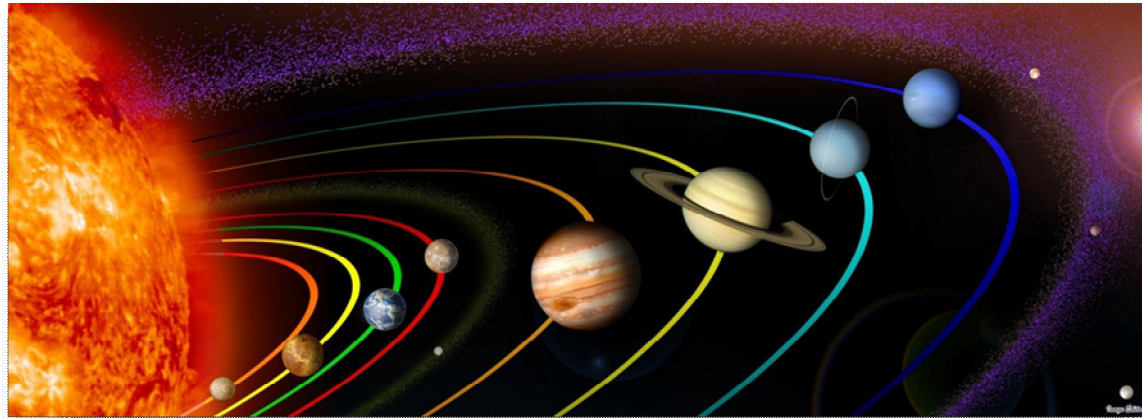


Image: Massachusetts Academy of Sciences

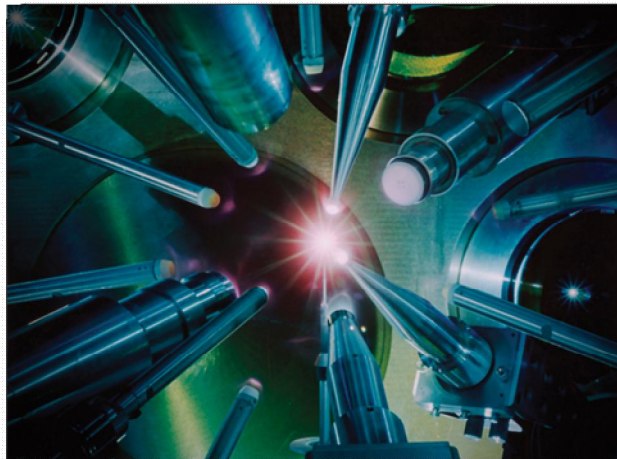


Image: Lawrence Livermore National Laboratory

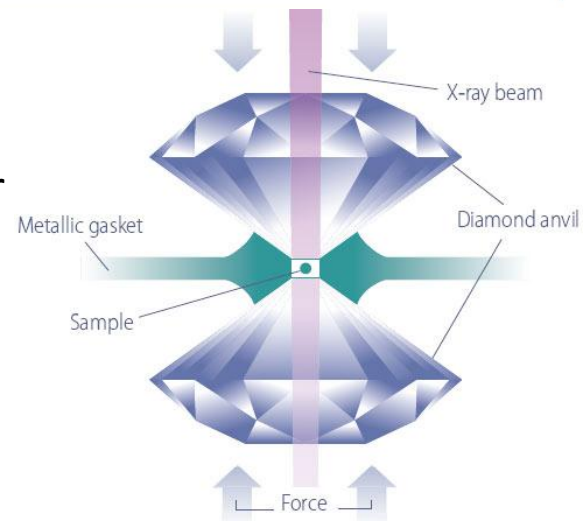
Moreover:

- Wanted: complete physical description
- Access to this regime only recently possible

HED: Generation in the Laboratory I

Static Pressure:

Isothermal pressure increase possible.
Maximum achieved pressure \approx 3-4 Mbar



Shock:

Dynamically reach higher pressures
Maximum achievable compression in a single shock limited! (\rightarrow Hugoniot-curves)

Examples for shock compression methods:

Flyer plate impact (gas guns, z-machine)
Laser shock compression (typ. ns-long, high-energy laser pulses)



HED: Generation in the Laboratory II

Energy deposition inside target:

via charged particles (protons, ions):

$$\frac{dE}{dx} \propto -\frac{n_e Z^2}{\beta^2} [\dots]$$

via x-rays:

$$\frac{dE}{dx} = -\mu_E(h\nu)$$

(Quasi-)Isochoric heating: heating process **faster than hydro-expansion**

Examples for quasi-isochoric heating via particles:

Heavy-ions at high ion beam intensities (HHT @ GSI, HIHEX and LAPLAS @ FAIR) (~ ns timescale)

Laser-generated protons or ions (~ ps timescale)

Laser-generated electrons (~ ps timescale)

Laser-generated Electrons I

Laser intensities about $\geq 1E18$ W/cm² ($|\vec{E}_{\max}| \geq 2.7E12$ V/m)

→ Electron energies

$$\langle E_{kin} \rangle = \frac{m_e}{2} \langle v^2 \rangle = \dots = \frac{1}{4} \frac{e^2 |\vec{E}_{\max}|^2}{m_e \omega^2} \approx 90 \sqrt{I_{18} \lambda_{\mu}^2} \quad [\text{keV}]$$

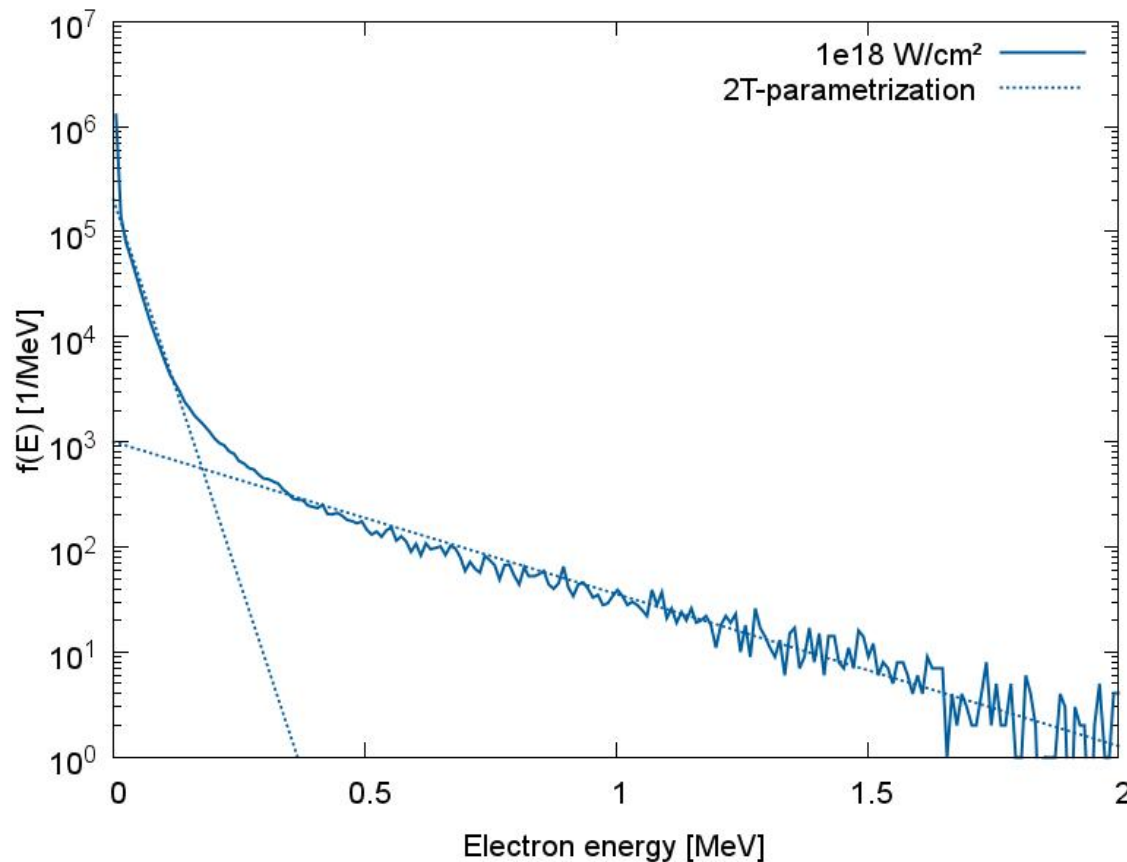
Laser-plasma interaction:

- inverse bremsstrahlung
- resonance absorption
- skin-layer heating
- Brunel-heating
- **J x B**-Heating
- Ponderomotive acceleration
- Anharmonic resonance
- ...

Dependent on plasma-gradients, intensity, polarization...

Laser-generated Electrons II

Simulation via **Particle-In-Cell (PIC)** codes.



$$f(E) \propto$$

$$\frac{\eta_1}{T_1} \text{Exp}[-E/T_1] + \frac{\eta_2}{T_2} \text{Exp}[-E/T_2]$$

Typical:

$$\eta \approx 10\%, T \approx 100\text{s} - 1000\text{s keV}$$

$$T_{Wilks} = 511 \left(\sqrt{1 + \frac{I_{18} \lambda_{\mu}^2}{1.37}} - 1 \right) [\text{keV}]$$

$$T_{Beg} = 100 \cdot (10 \cdot I_{18} \lambda_{\mu}^2)^{1/3} [\text{keV}]$$

Calculations performed by A. Karmakar, P. Gibbon, FZ Jülich

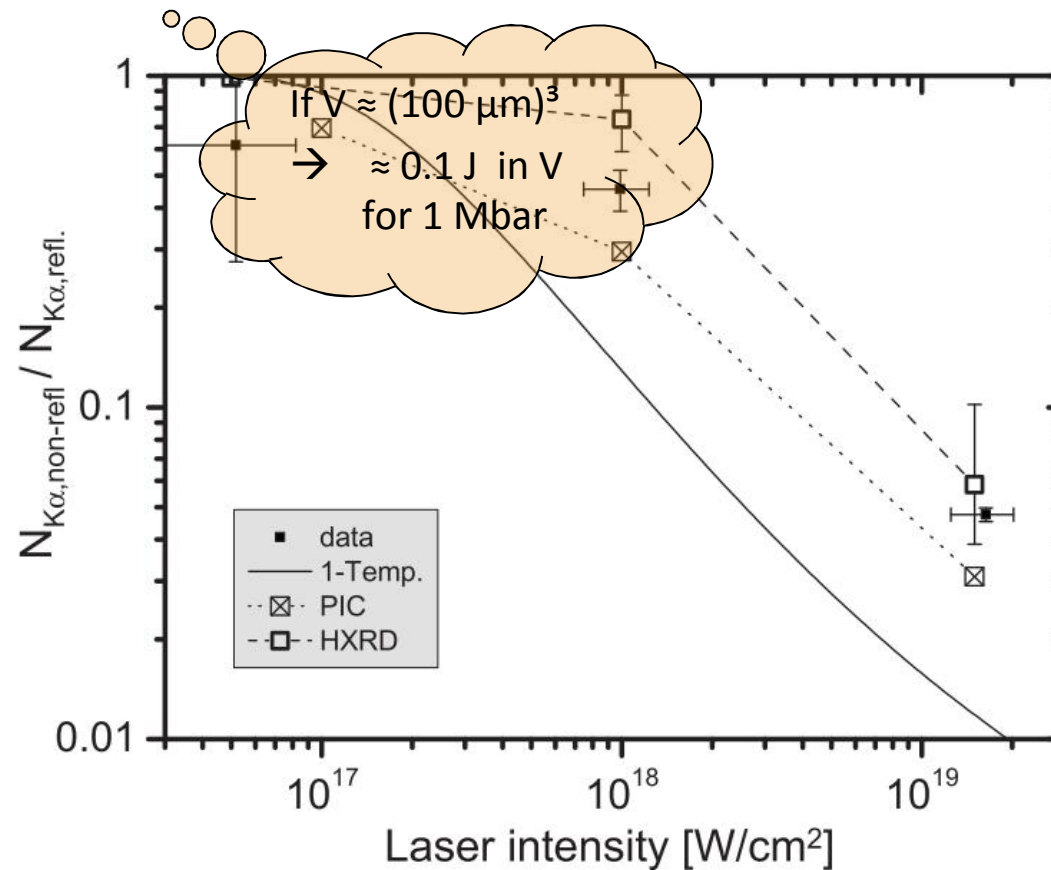
Electrons in a Cage

Typical electron energies: 100 keV – 10 MeV → Range in solids ≈ mm to dm

How can we deposit the energy in a small volume?

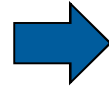
→ **Refluxing** of the hot electrons can be responsible for >95% of K_α and X-ray yield!

P. Neumayer et al., The role of hot electron refluxing in laser-generated K-alpha sources, Physics Of Plasmas 17, 103103 (2010).



Recipe: HED Via Isochoric e⁻-Heating I

Prepare a small, free-standing target (foil, wire, droplet etc.)



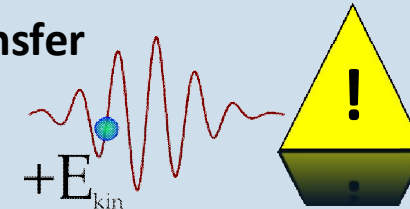
Focus a high-energy laser onto the target



Energy deposition
inside the
target volume



Energy transfer
Laser → e⁻



Expansion
($v \approx v_s \sim 30 \text{ km/s}$
 $= 30 \mu\text{m/ns}$)



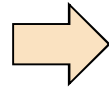
Recipe: HED Via Isochoric e⁻-Heating II

Physics of...

Responsible for...

Measured by...

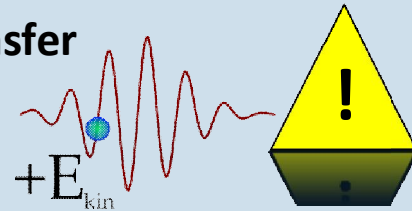
Laser absorption, hot electron generation



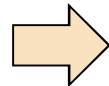
Energy transfer

Laser → e⁻

+E_{kin}

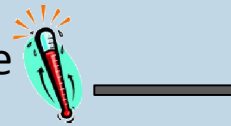


Electron transport, return currents etc.

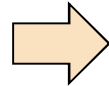


Energy deposition

inside the target volume

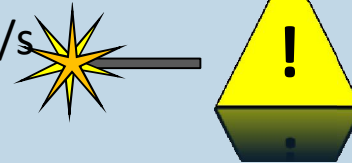


Fluid dynamics, EOS



Expansion

($v \approx v_s \sim 30 \text{ km/s}$
= 30 μm/ns)

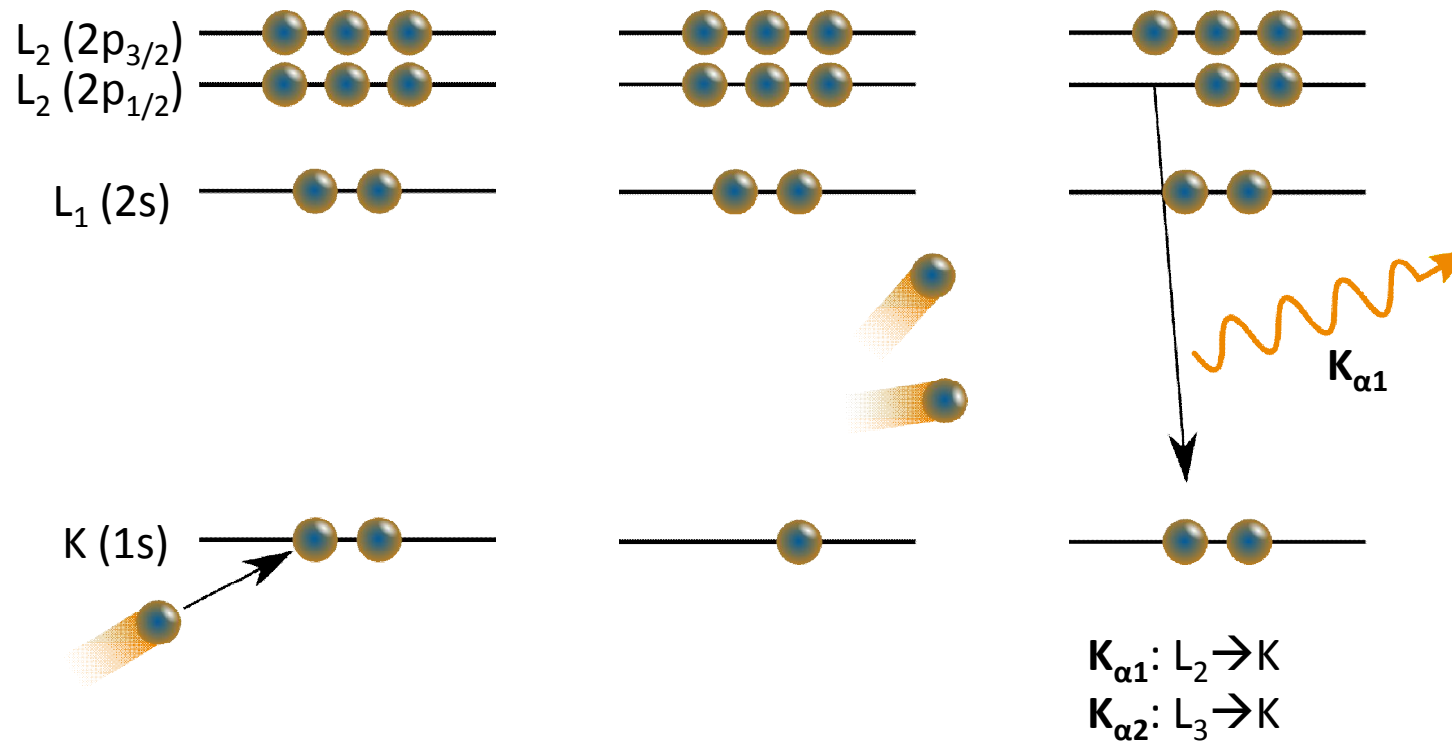


Spatially resolved K_α-spectrometry

X-ray radiography

Reminder: K_{α} -Radiation

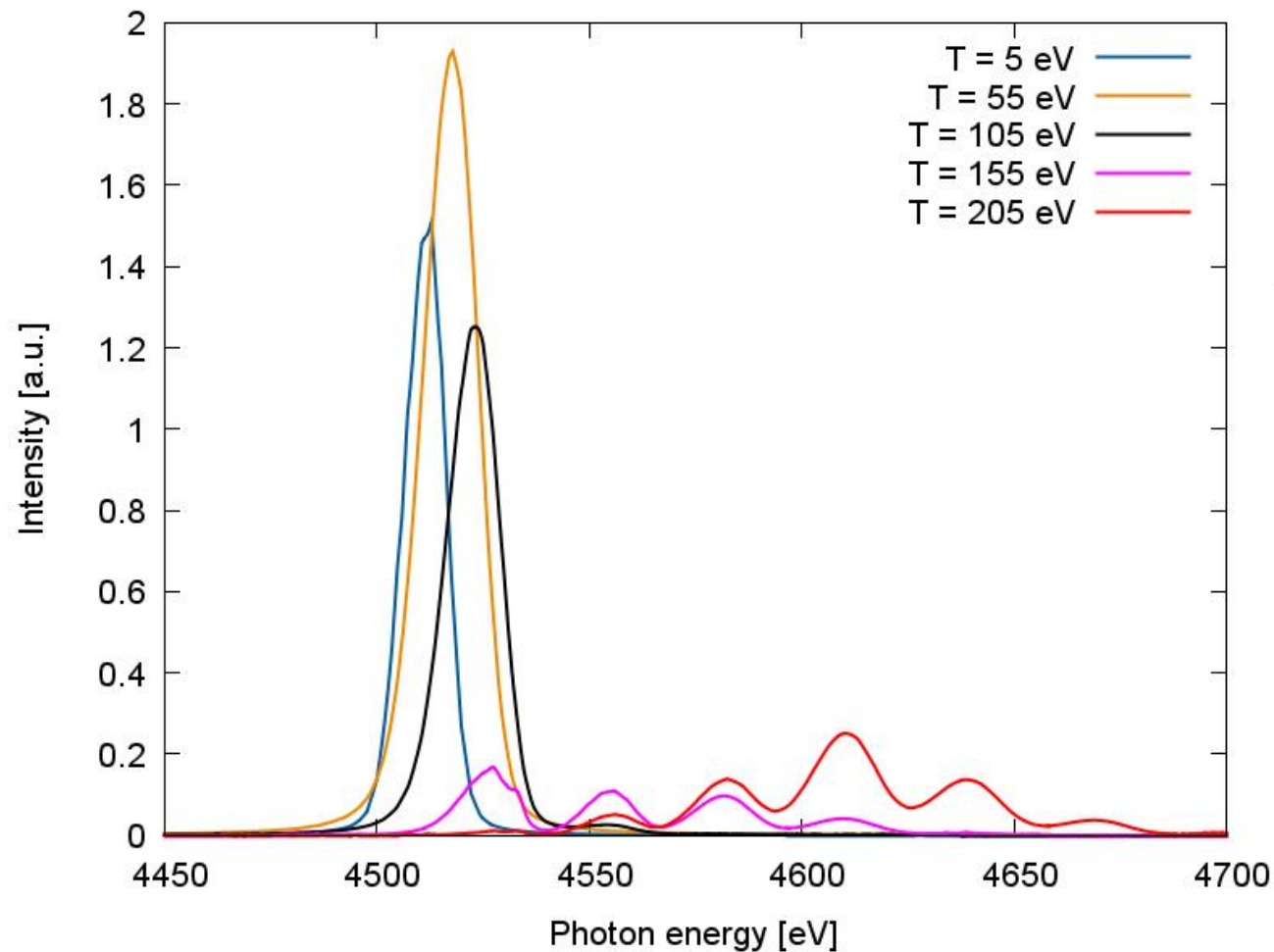
Line emission characteristic for material, charge state and temperature



K_{α} -signal at X \rightarrow electron ($E \geq E_{K\text{-ionization}}$) passed X

K_{α} -spectrometry

Atomic kinetics simulation (FLYCHK) for Ti @ solid density



Higher T

→ ionization

Different energy levels in
different ion species

→ appearance of satellites

X-ray Radiography: Requirements

Radiography = taking photographs of the inside of a sample at different waiting times after start of expansion

Typical sample size $L \approx 10 - 100 \mu\text{m} \rightarrow$

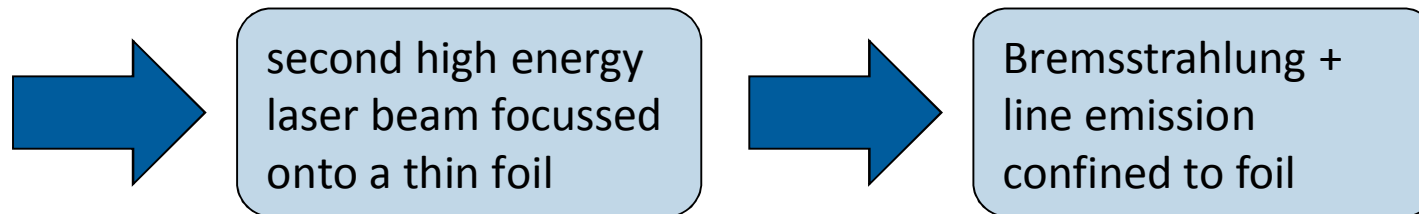
- **spatial resolution** better than L
- **time resolution** better than $\approx L/v_s = 0.3 - 3 \text{ ns}$

$n_e < n_c(h\nu)$ and reasonable opaqueness \rightarrow

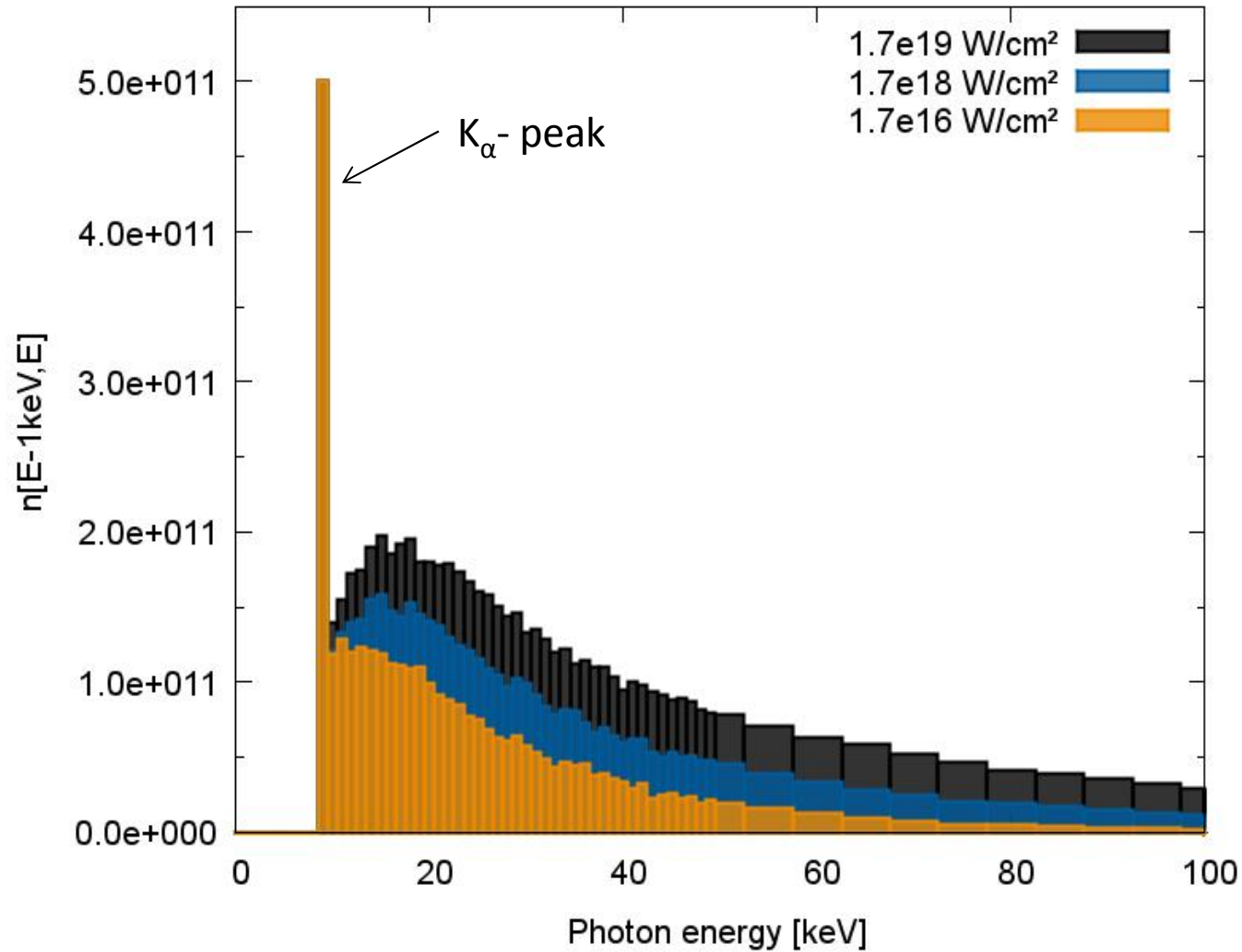
- **$h\nu \approx 1 - 10\text{s of keV}$** (intermediate x-rays)

Photon number of „imager“ \geq self emission of target \rightarrow

- **bright** backlighter



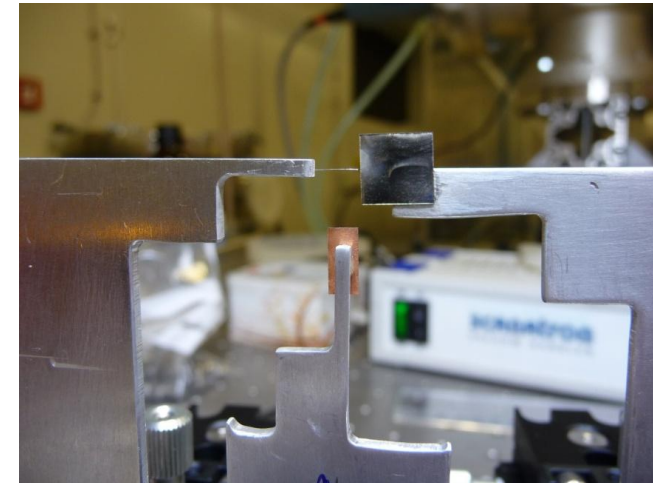
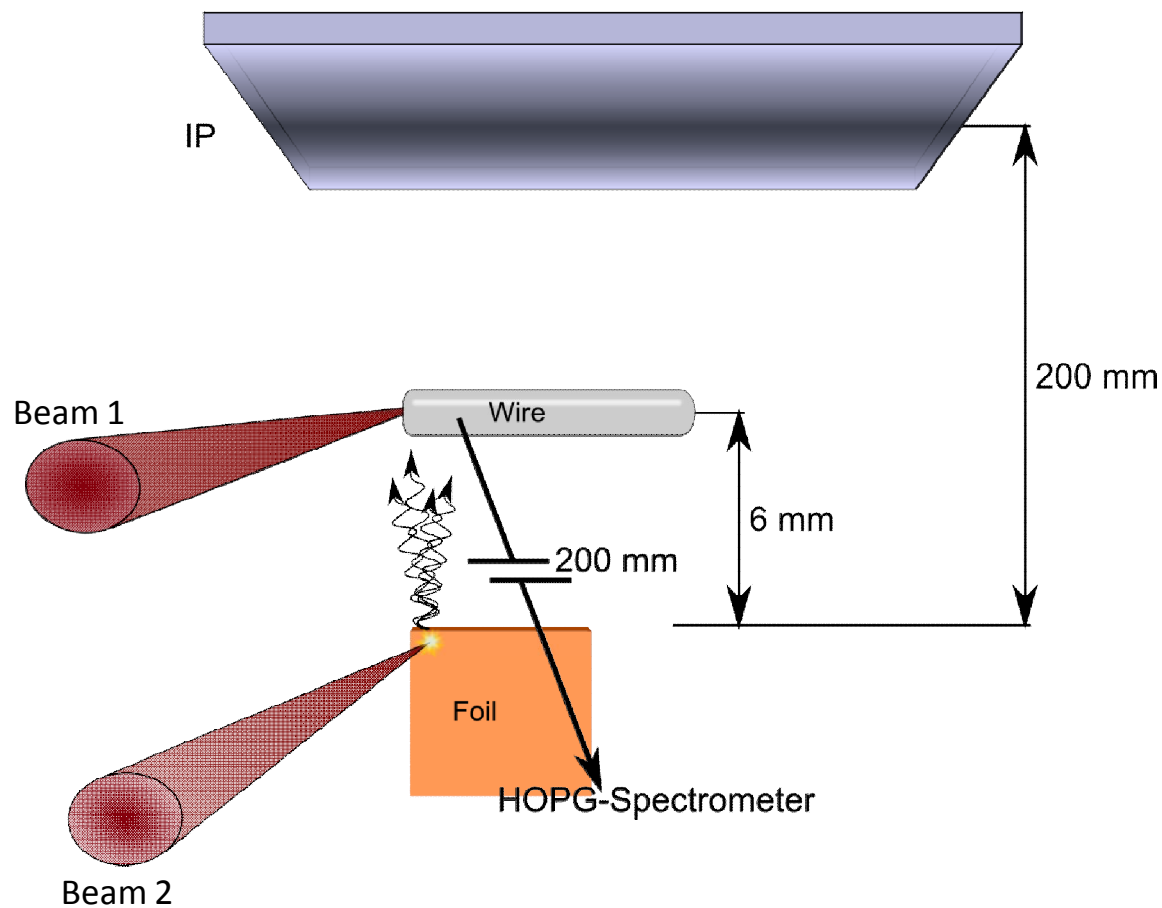
X-Ray Radiography: Imaging Spectrum



Spectrum must be known to extract densities from radiograph!

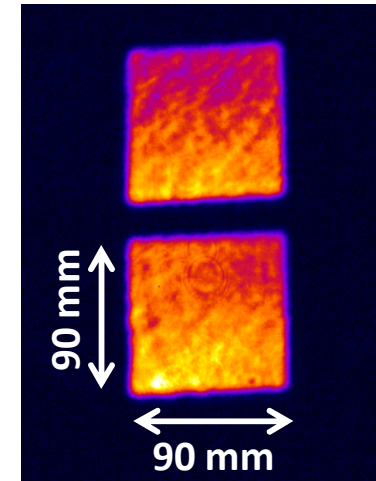
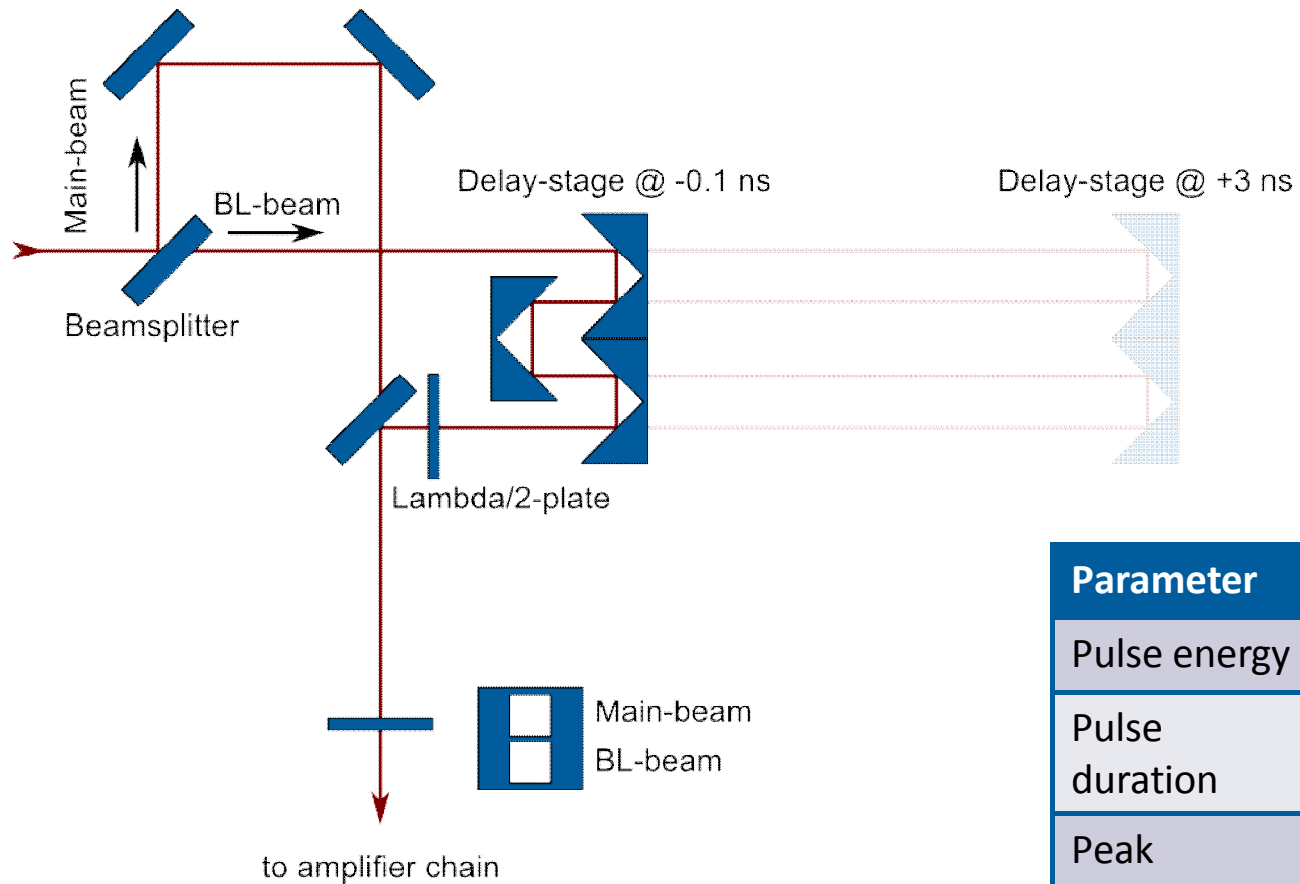
Experiment: Target Setup

WDM-target: Ti – Wire (d = 50 & 80 μm , L = 5mm)
Backlighter-target: Cu – Foil (d = 3 & 7.5 μm)



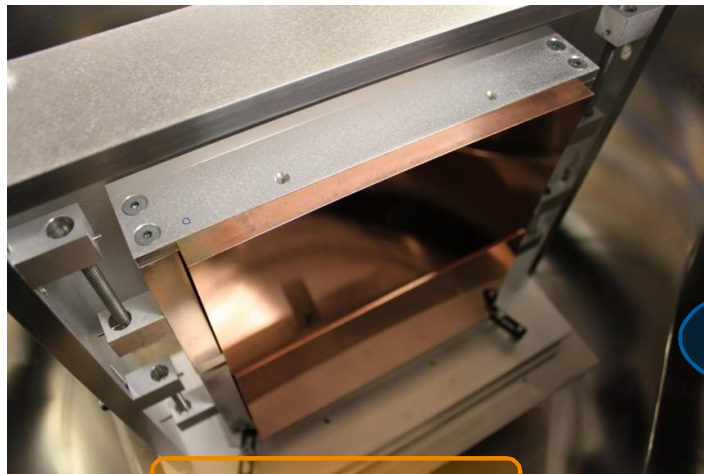
Experiment: Double-Beam

Schematic of the double-beam setup



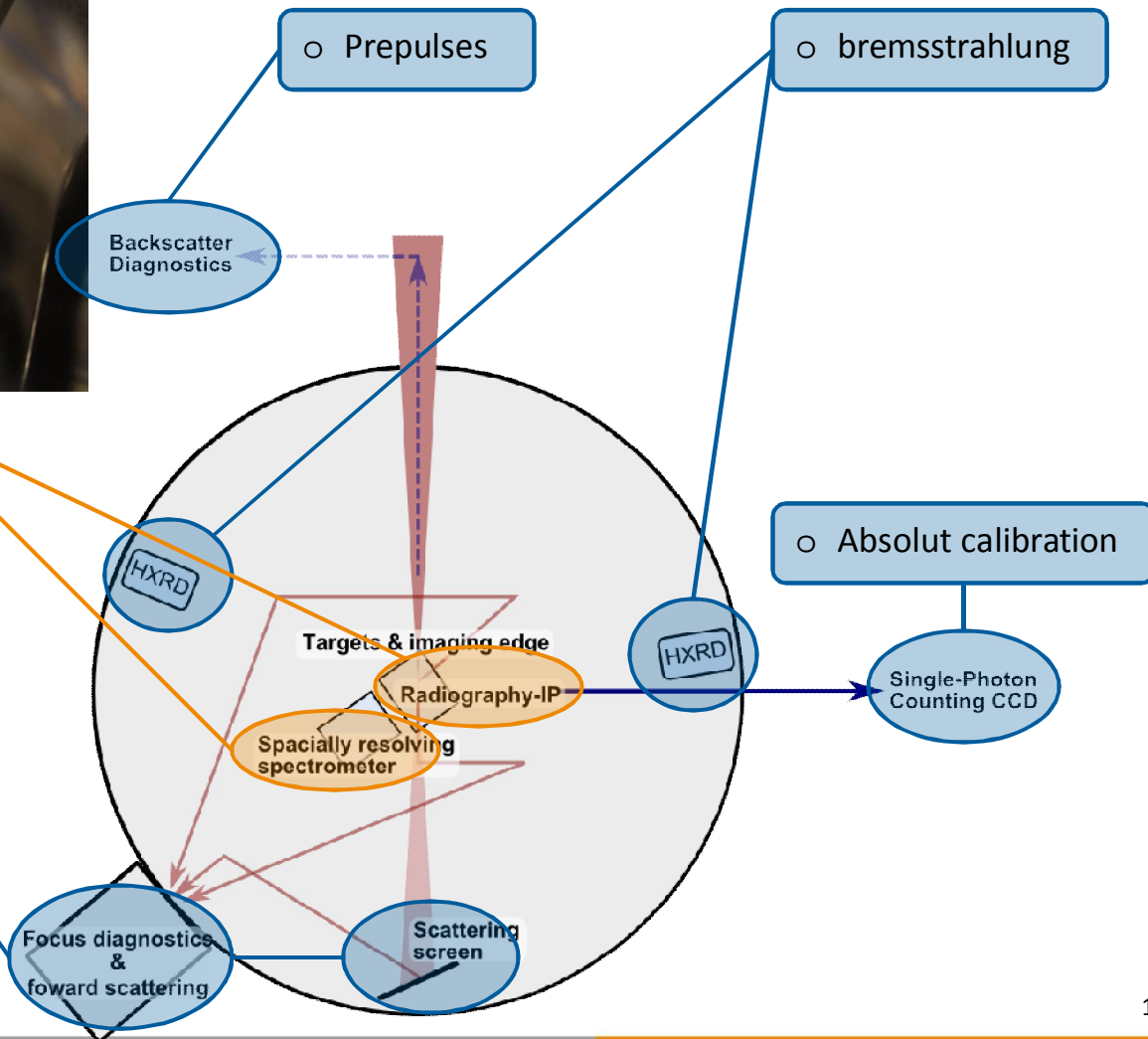
Parameter	Beam 1	Beam 2
Pulse energy	Up to 50 J	Up to 50 J
Pulse duration	500 fs to 8.5 ps	500 fs to 8.5 ps
Peak intensity	3E17 – 8E18 W/cm ²	≤1.5E17 W/cm ²

Experiment: Diagnostics

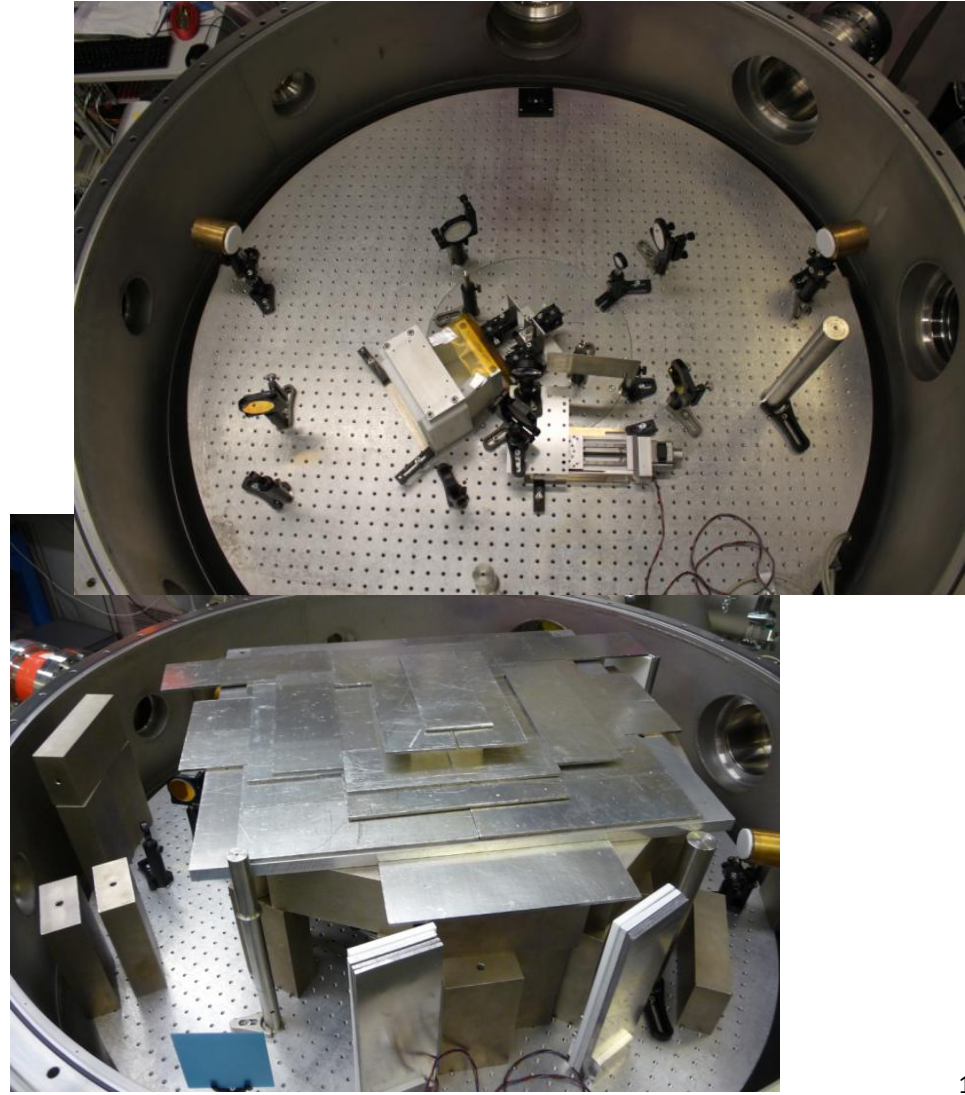
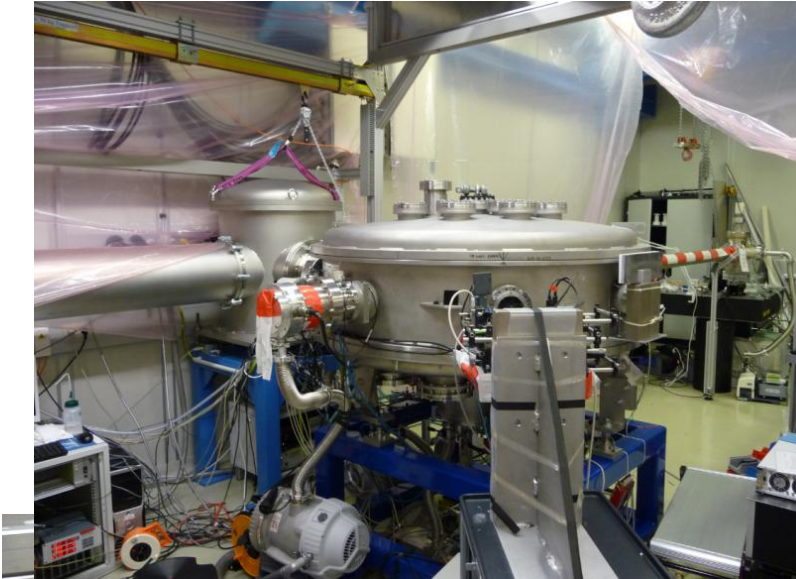


○ Main Diagnostics

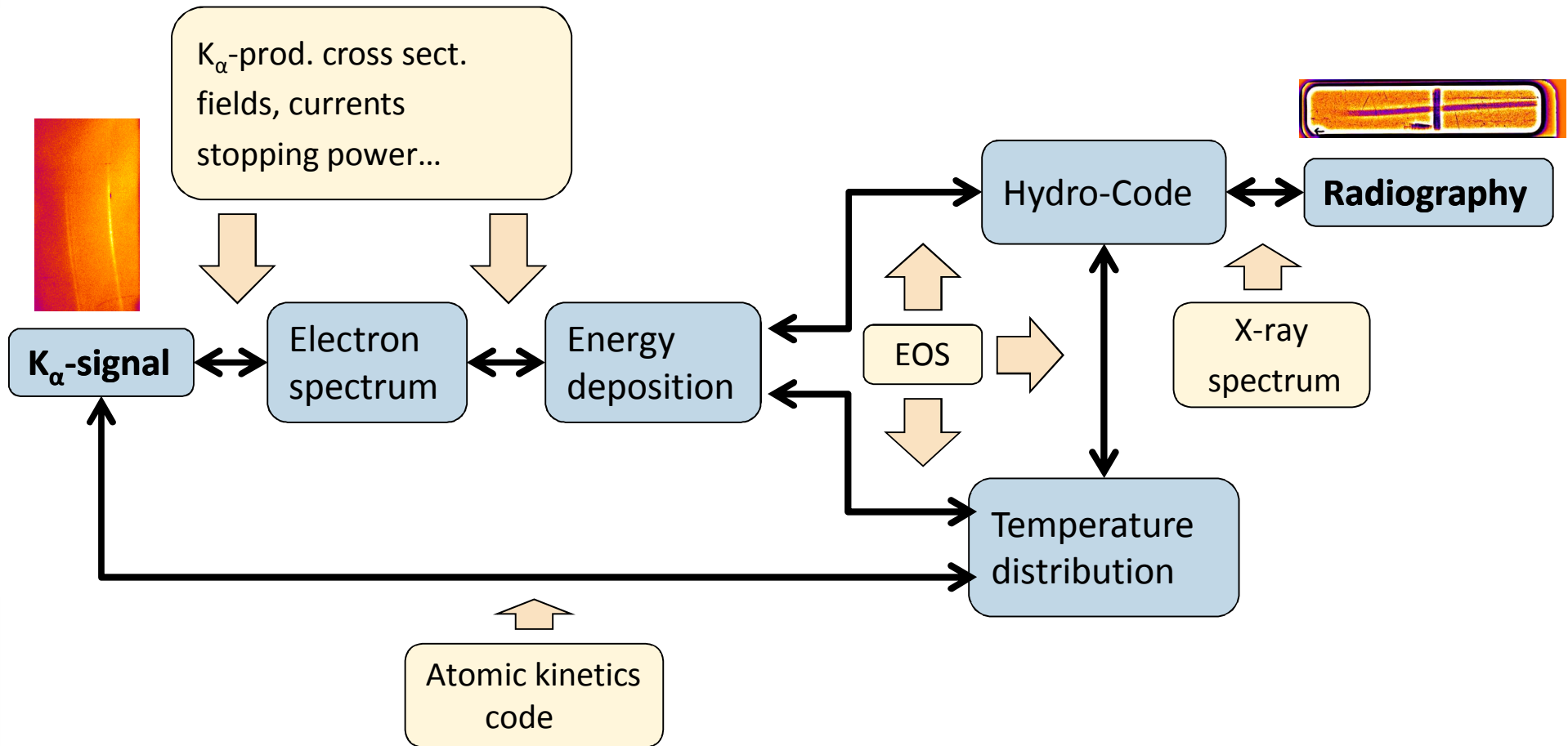
- Focussing parameters
- Missed energy



Experiment: Impressions



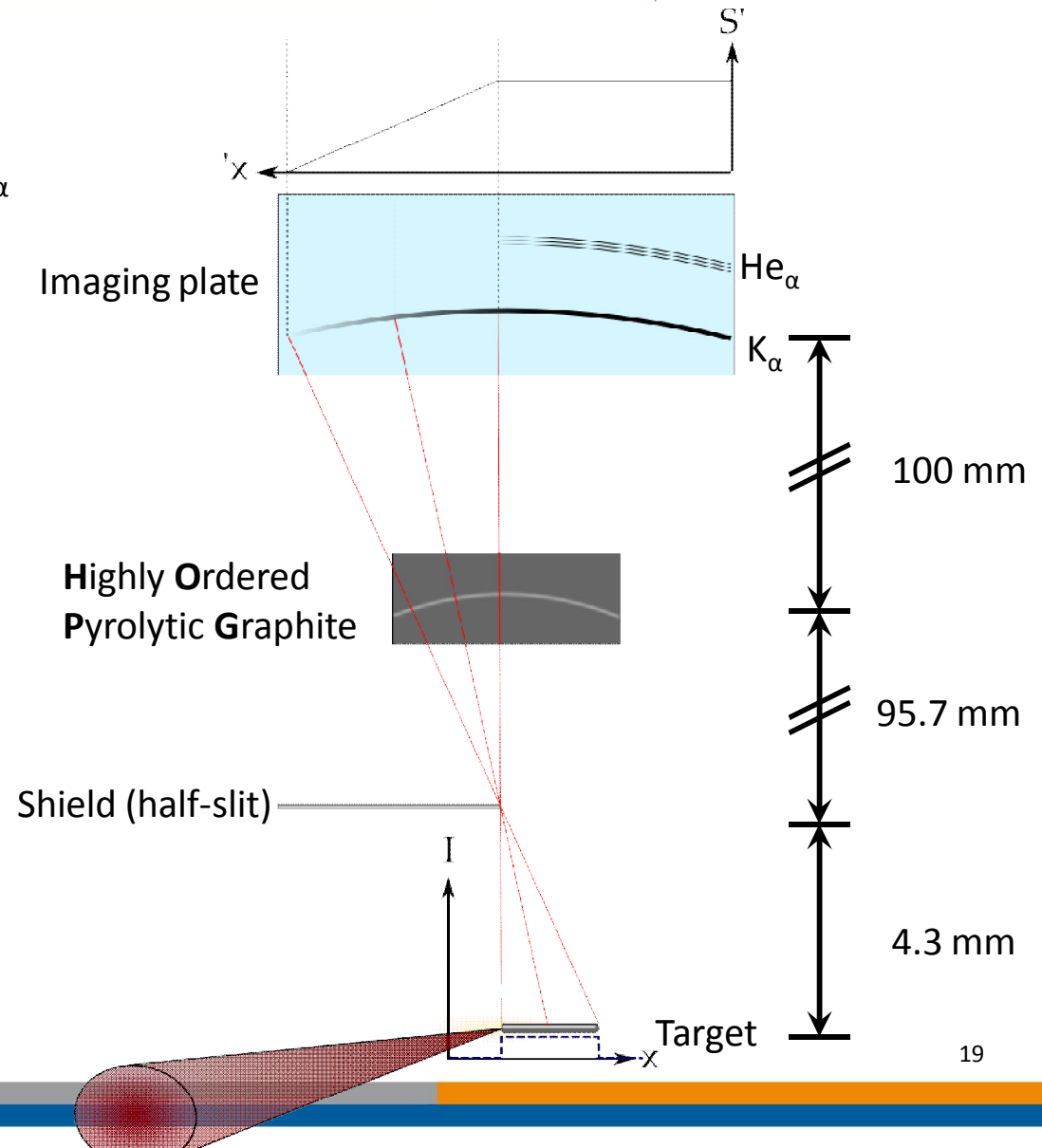
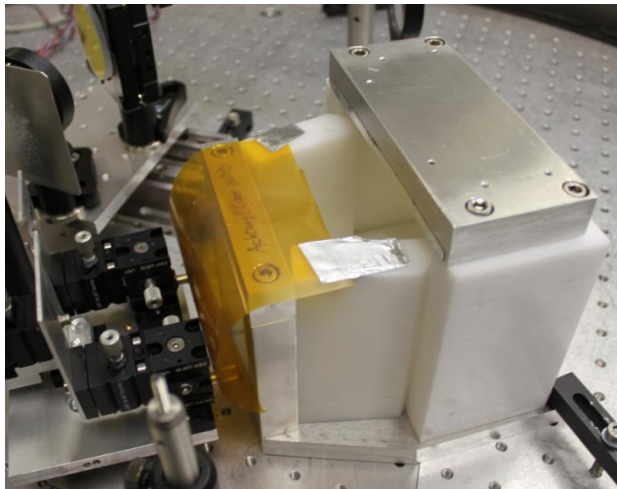
Analysis



Analysis: HOPG Spectrometer

- Resolution 25 μm
- Magnification ≈ 45
- Spectral coverage Ti- K_α up to Ti He $_\alpha$

$$S'(x') = \int_{-\infty}^{x_0(x')} dx S(x)$$



Analysis: Hot Electron Spectrum I

Parametrized according to $f(E) \propto \frac{\eta_1}{T_1} \text{Exp}[-E/T_1] + \frac{\eta_2}{T_2} \text{Exp}[-E/T_2]$

Self-developed collisional model (1D) including:

- relativistic K_α -production cross section
- ESTAR stopping power
- ohmic heating
- refluxing
- EOS for temperature (PROPACEOS)

not including:

- self-consistent electric and magnetic fields
- multi dimensional effects

Analysis: Hot Electron Spectrum II

Shot 34

Example: shot 34

Experiment:

$$E_{\text{laser, eff}} = 36.7 \text{ J}$$

$$d_{\text{wire}} = 50 \text{ } \mu\text{m}$$

$$\eta_{\text{laser} \rightarrow \text{K}\alpha} = 3.9\text{E-}4$$

$$\#_{\text{K}\alpha\text{-photons}} = 2\text{E}13$$

Best fit:

$$\eta_1 = 12.5 \%$$

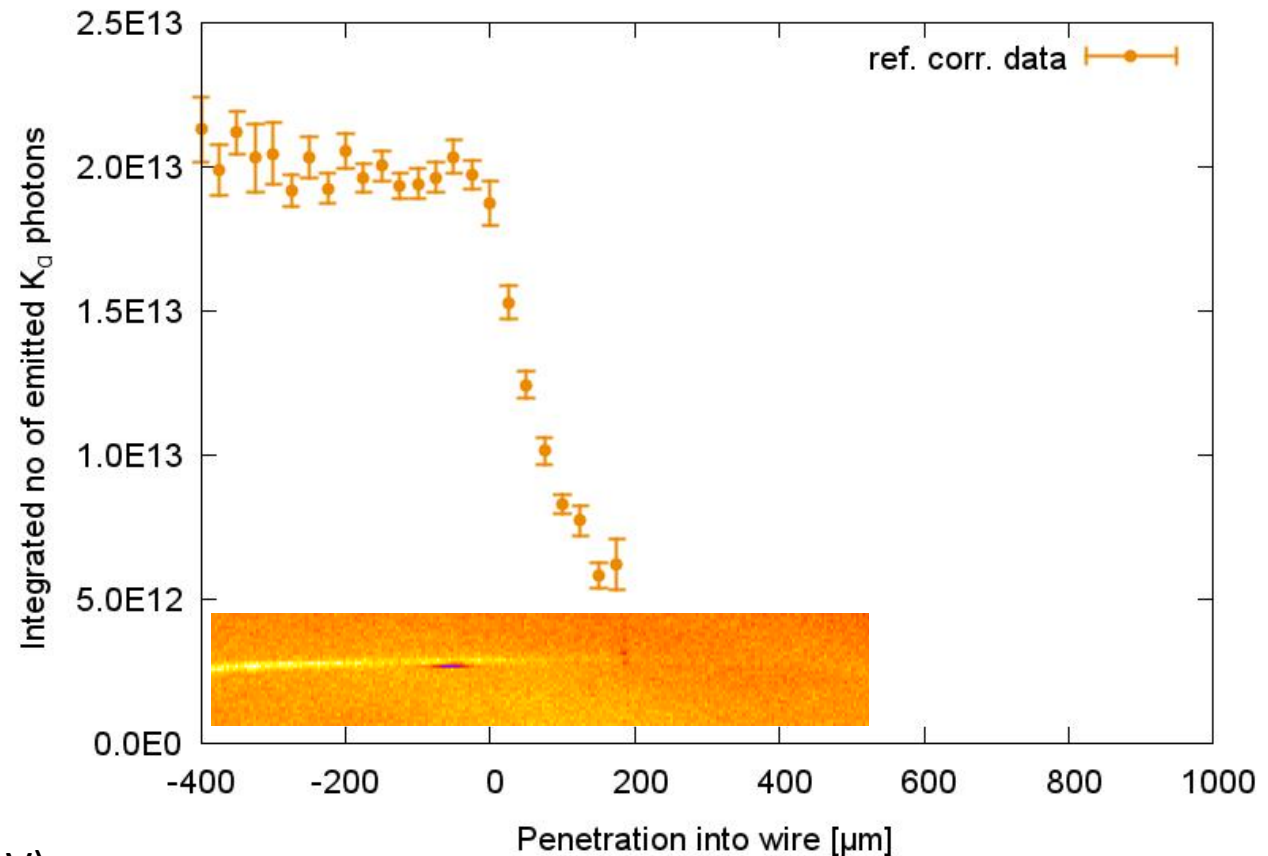
$$\eta_2 = 1.5 \%$$

$$T_1 = 110 \text{ keV}$$

$$T_2 = 400 \text{ keV}$$

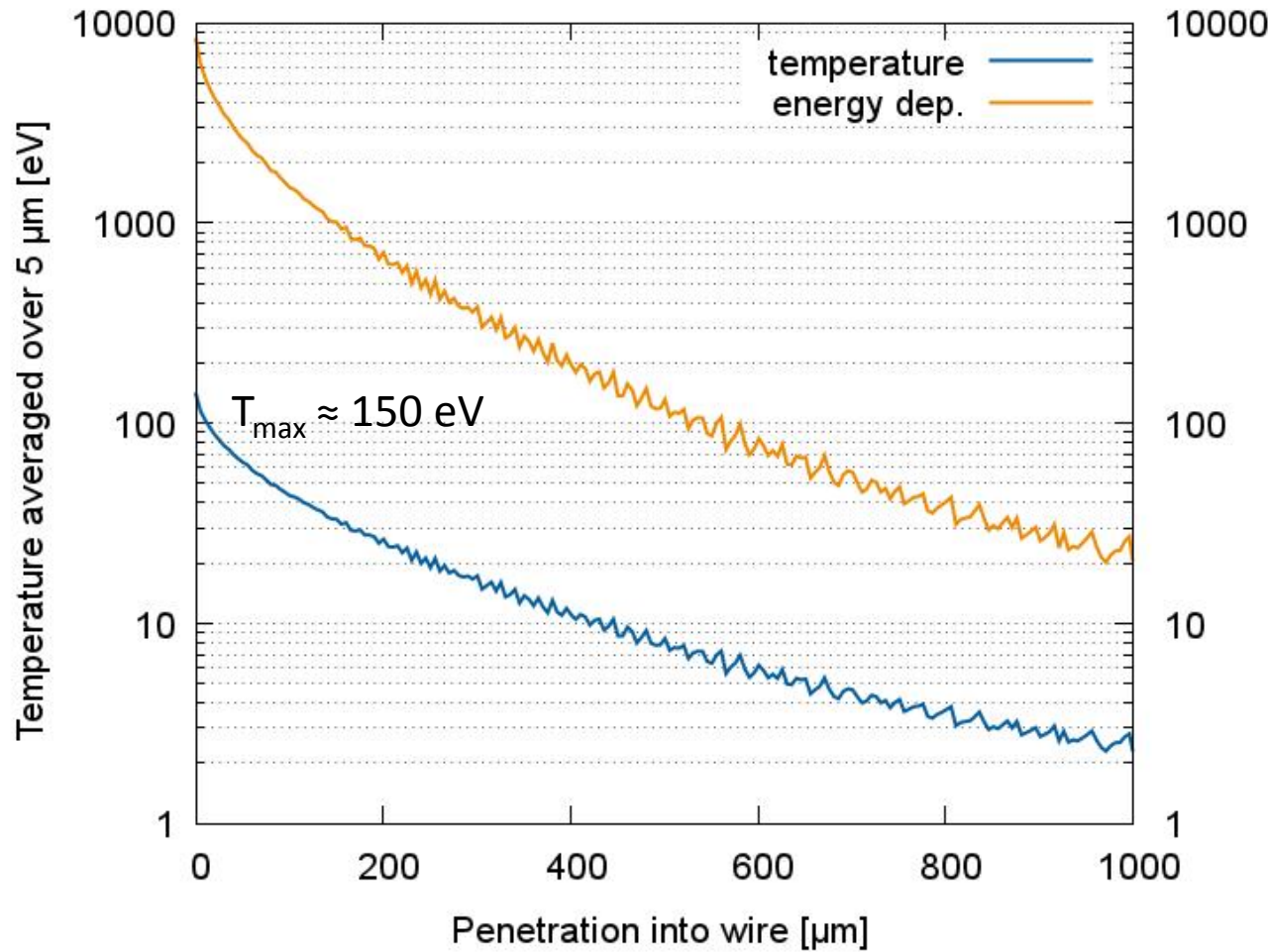
(Wilks: 105 keV, Beg: 184 keV)

max. current \approx 200 kA



Analysis: Energy Deposition

Shot 34

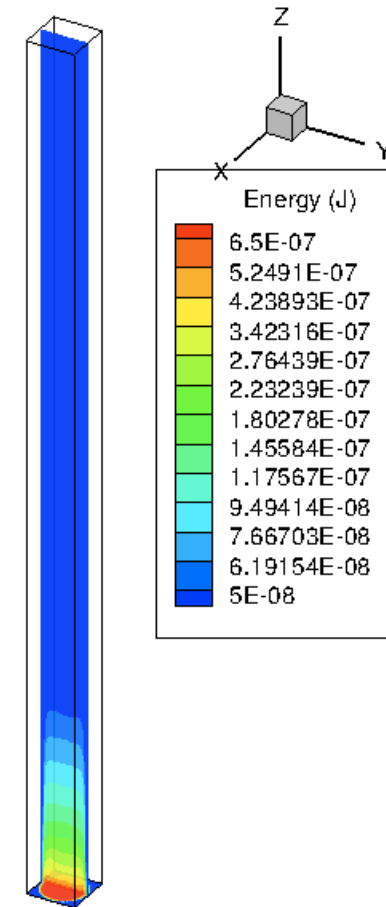
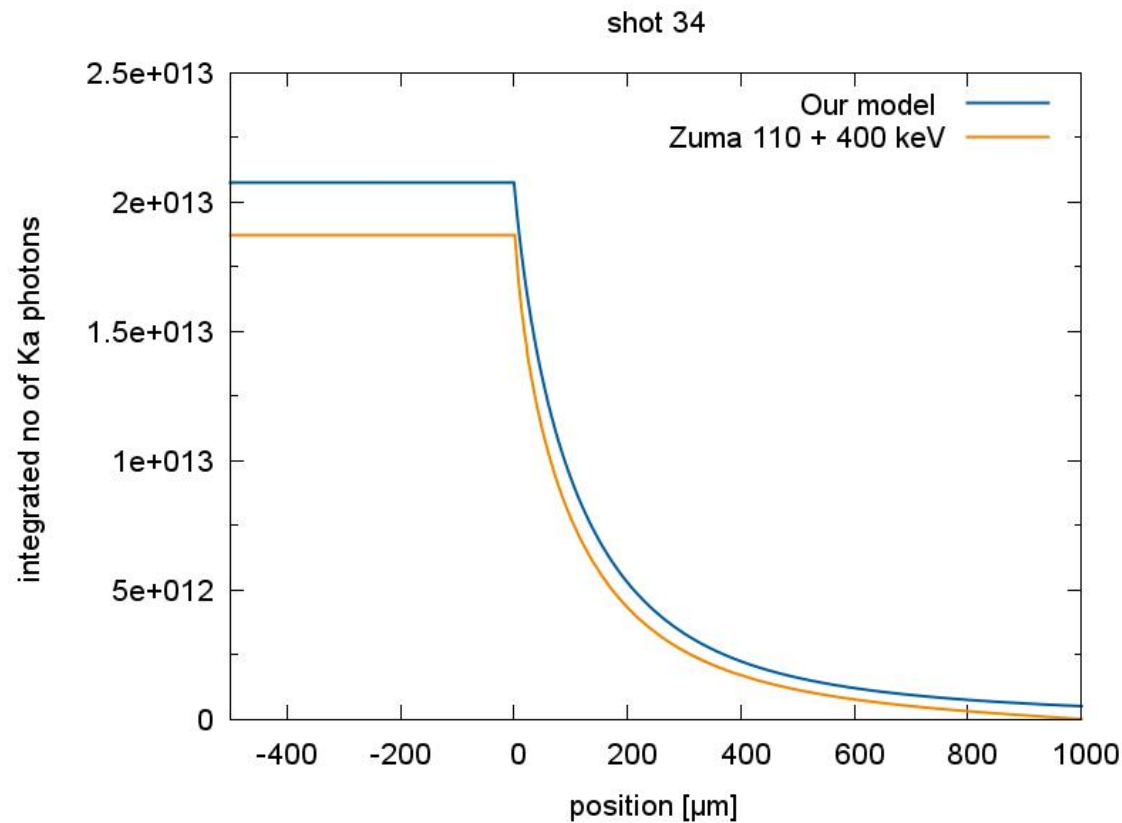


→ Relation
Temp. <-> Space
En. Dep. <-> Space

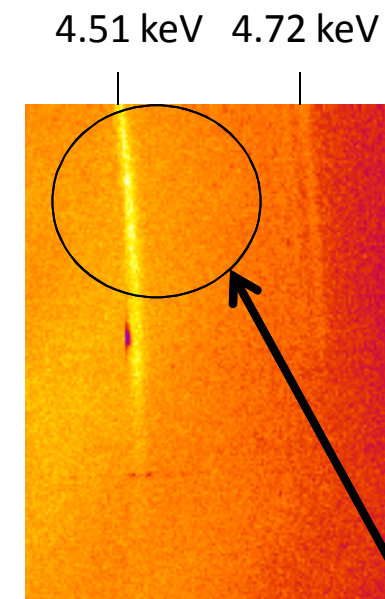
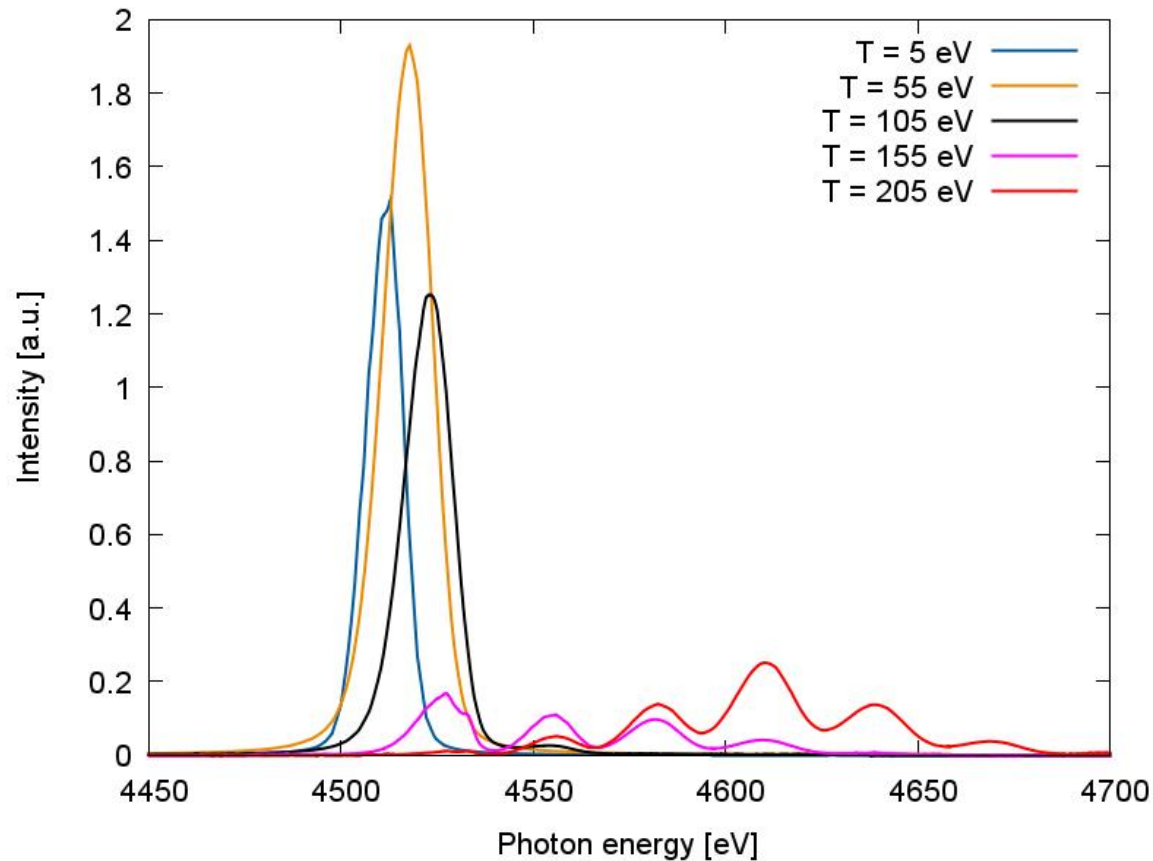
Comparison to 3D Hybrid PIC Code

ZUMA: Modelling electron transport in 3D including fields, return currents etc.

K_{α} production



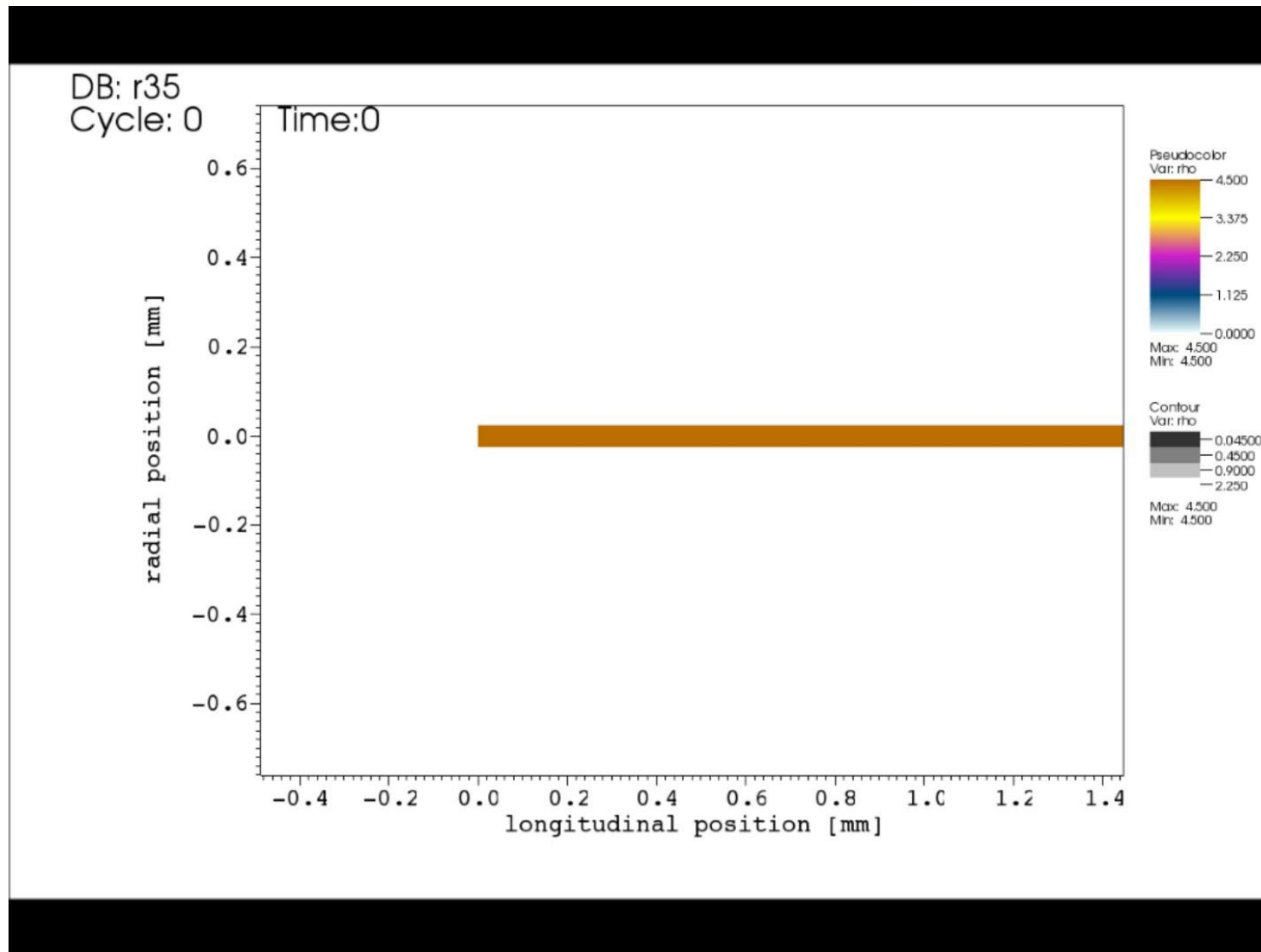
Analysis: Spectral Properties of Ti- K_{α}



No satellites!
 $T_{\max} \approx 150 \text{ eV} ?$

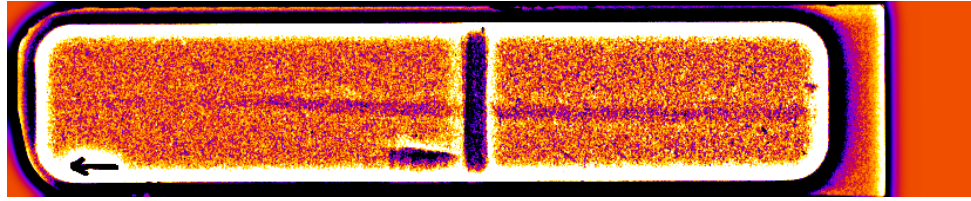
$\rightarrow T < 300 \text{ eV}$

Hydrodynamics: RALEF-2D Simulation

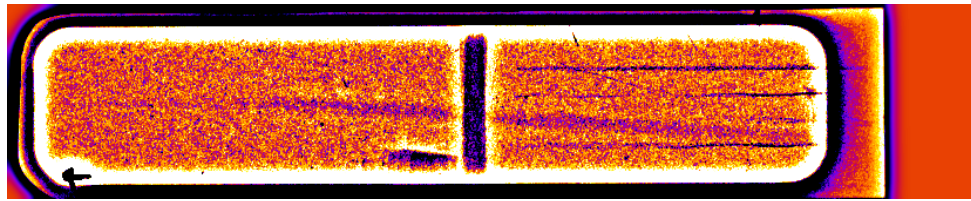


Hydrodynamics: Qualitatively

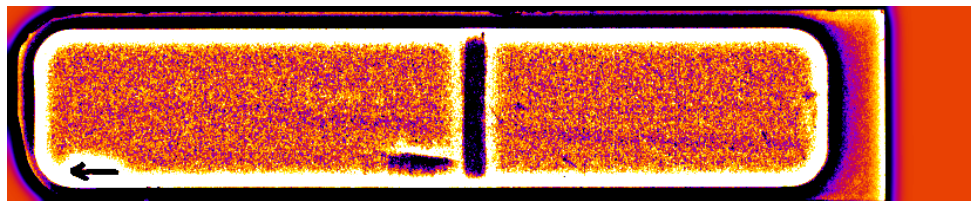
0.5 ns



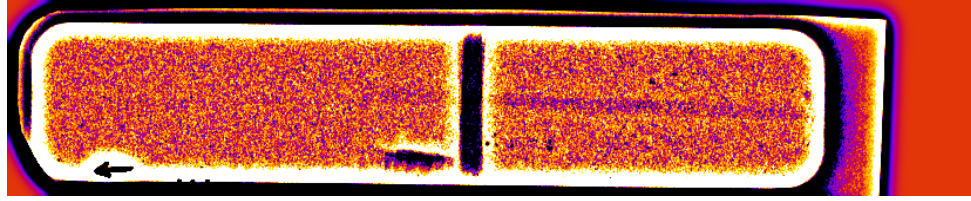
1.5 ns



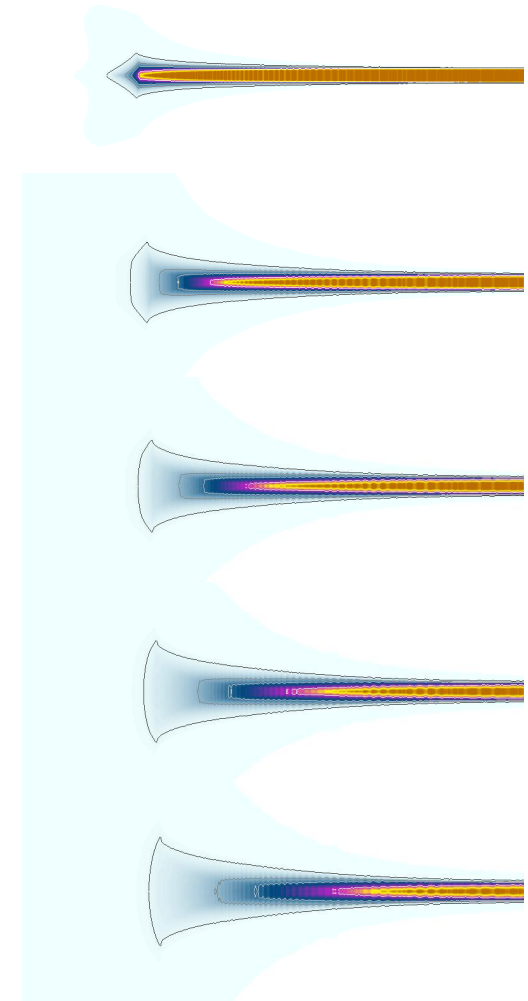
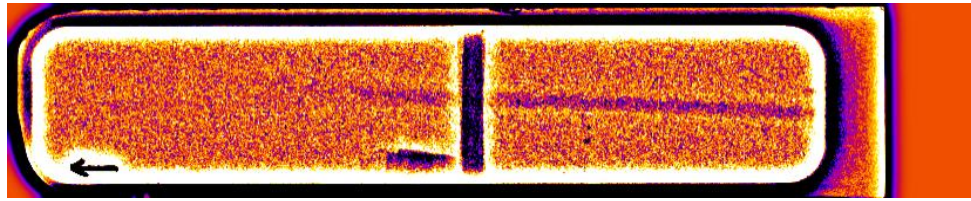
2.0 ns



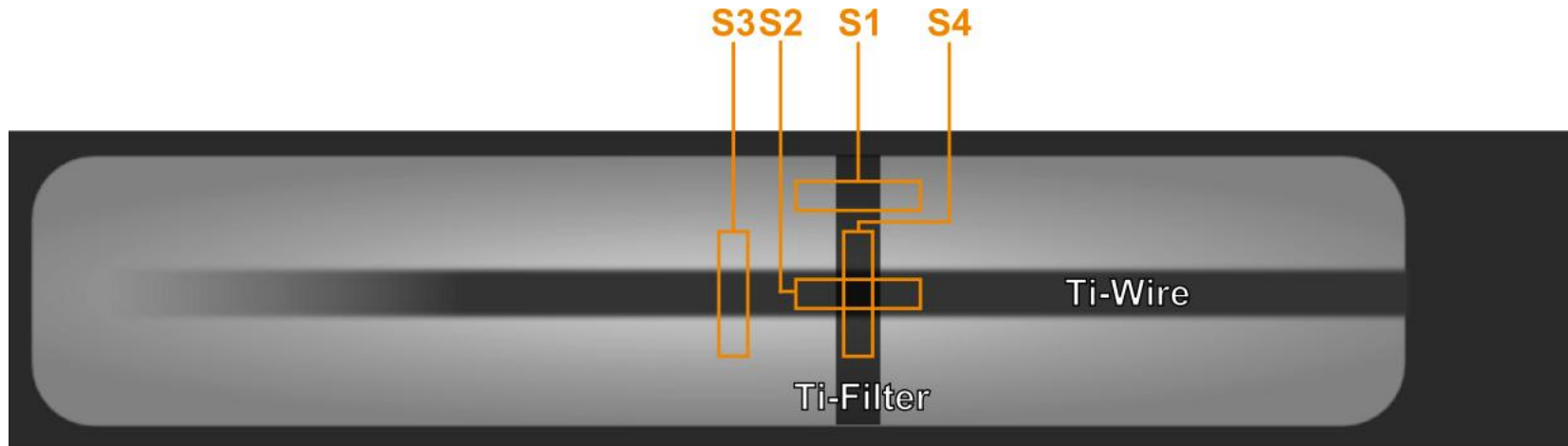
2.5 ns



3.0 ns



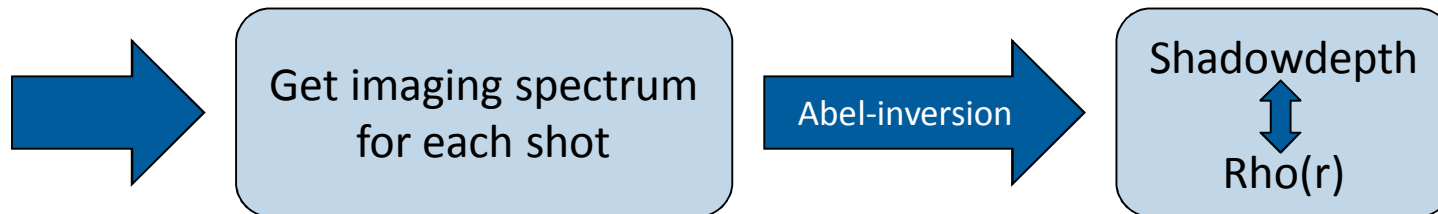
Hydrodynamics Quantitatively



- Testshots: Resolution: $(19 \pm 2) \mu\text{m}$ (transversal) x $(60 \pm 10) \mu\text{m}$ (longitudinal)

Important: imaging Spectrum?

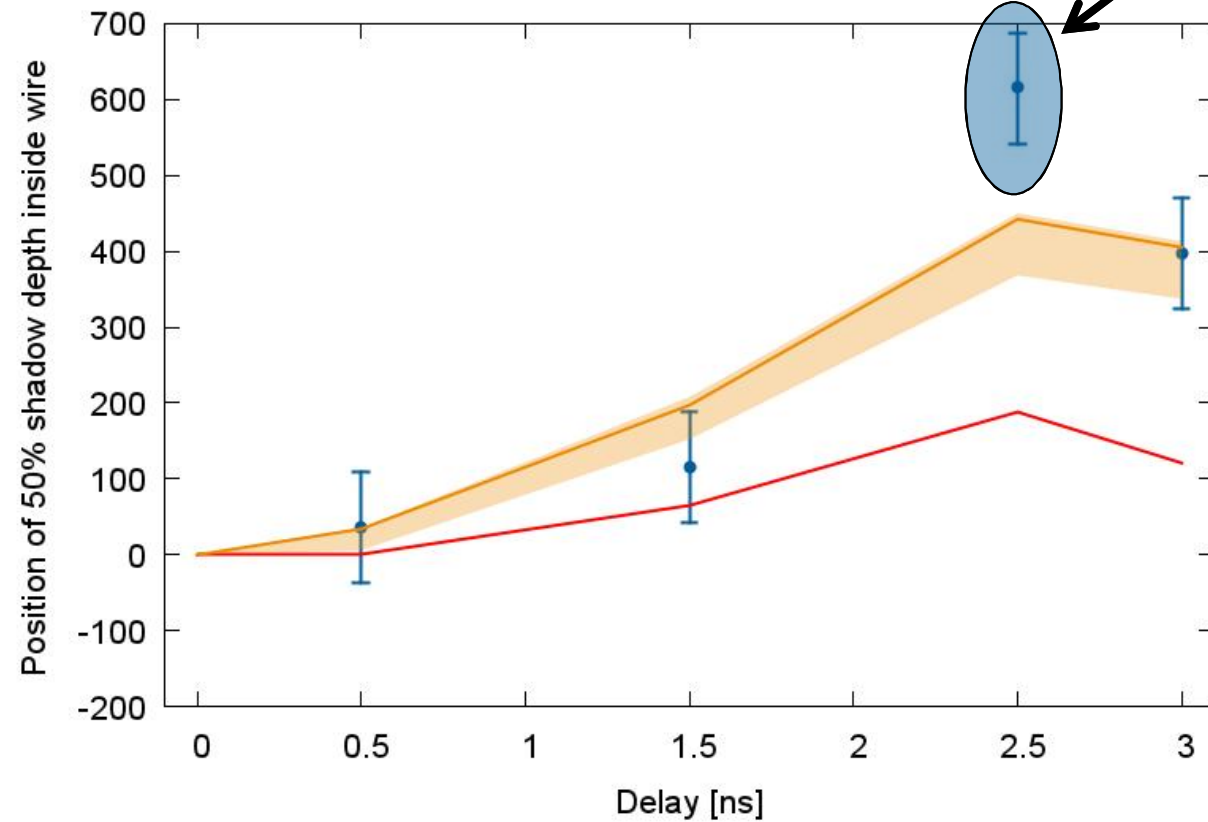
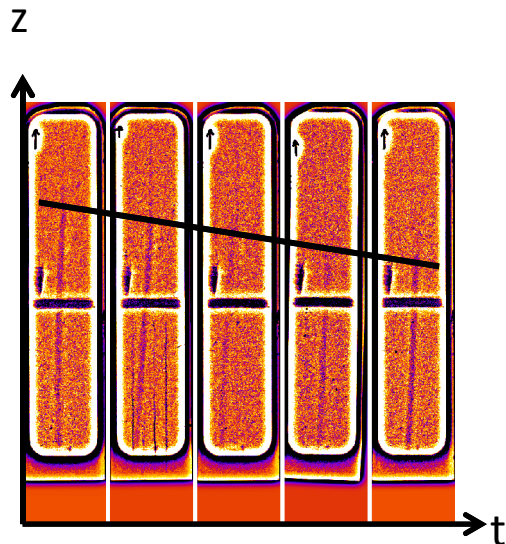
- Comparison of „shadowdepths“ for different lineout positions and directions
- Distinguish between imaging radiation and background



1D Hydrodynamics: „Burning“-Speed

Results of 1D hydro simulation using HELIOS code

Larger prepulse

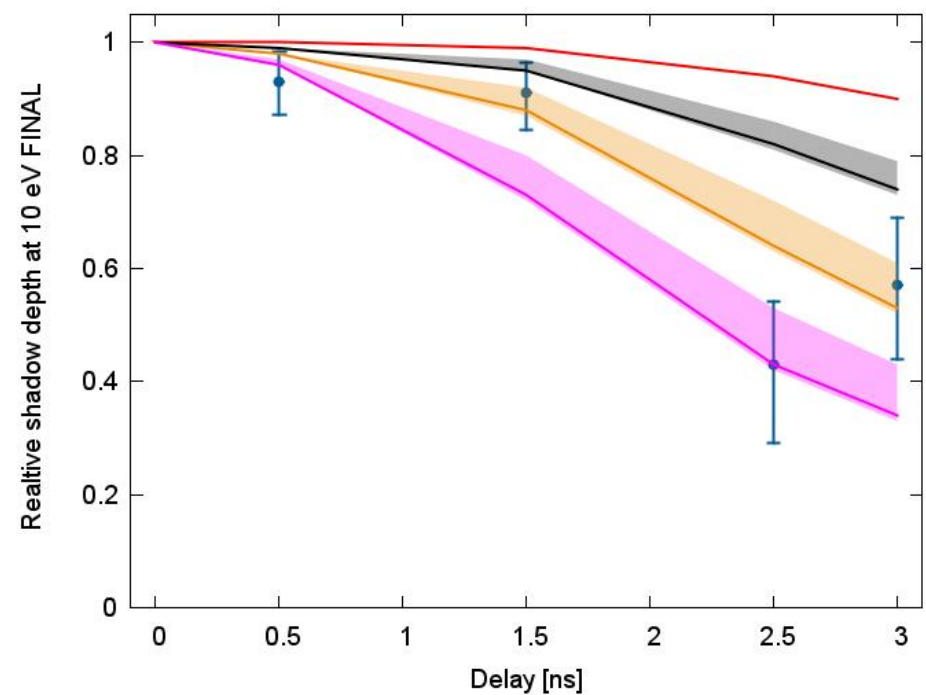
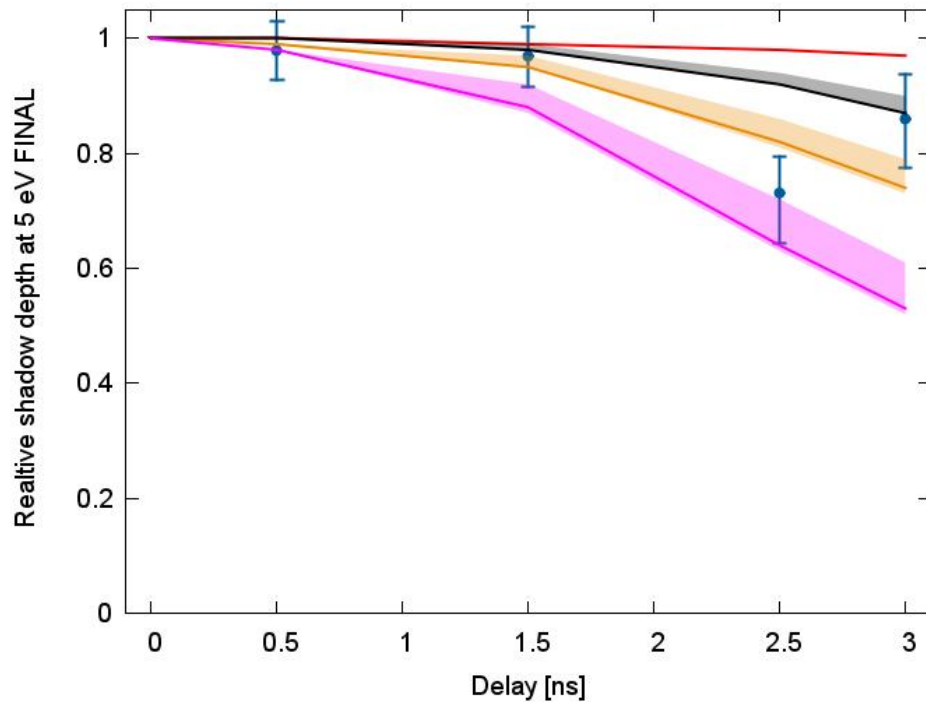


Exp. data  Simulation with Ka only  Simulation at 1x T 

1D Hydrodynamics: Fixed Initial Temperature

$T_0 = 5 \text{ eV}$

$T_0 = 10 \text{ eV}$

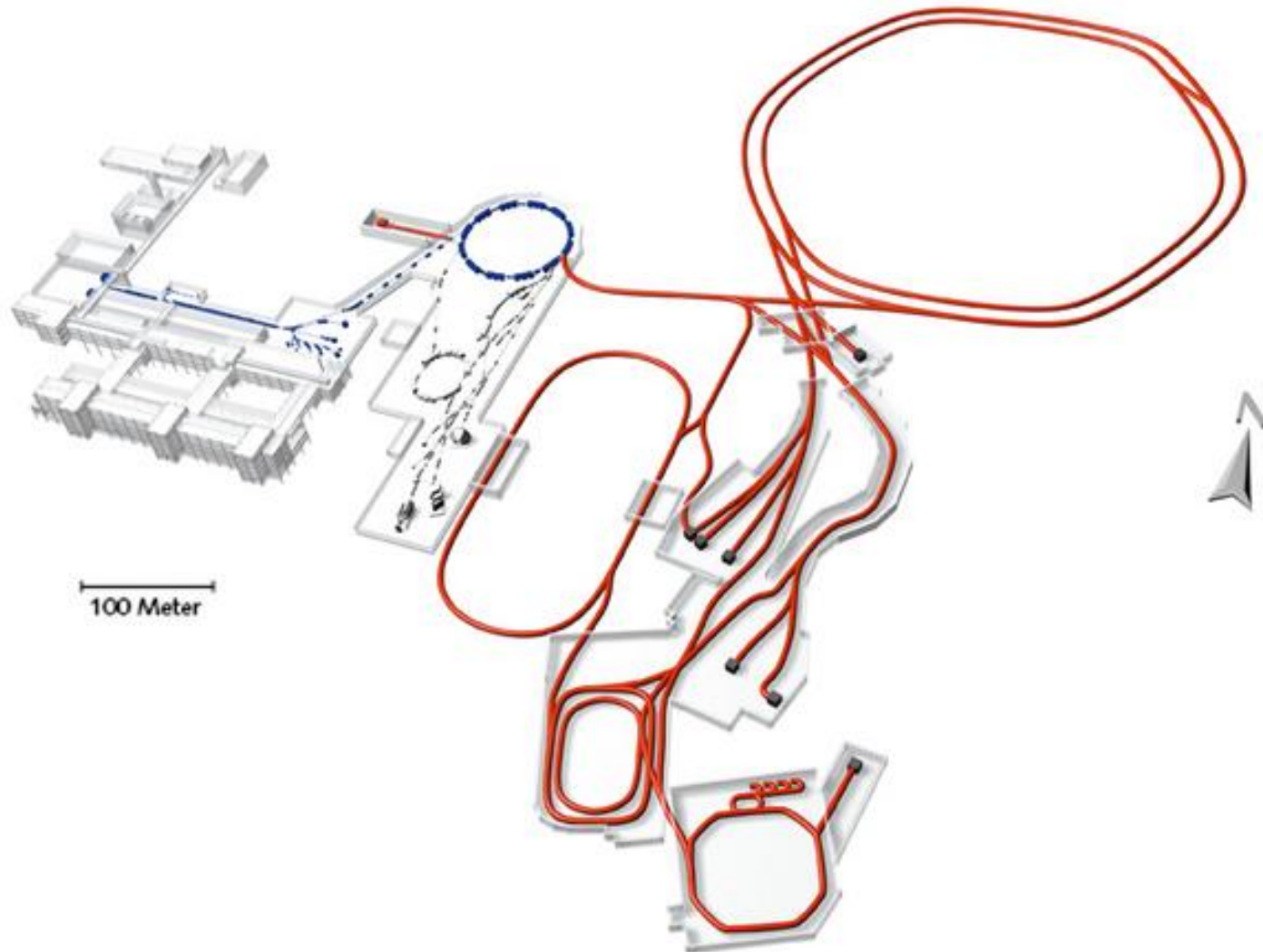


Experiment Simulation at 0.5x T
 Simulation with Ka only Simulation at 2x T
 Simulation at 1x T

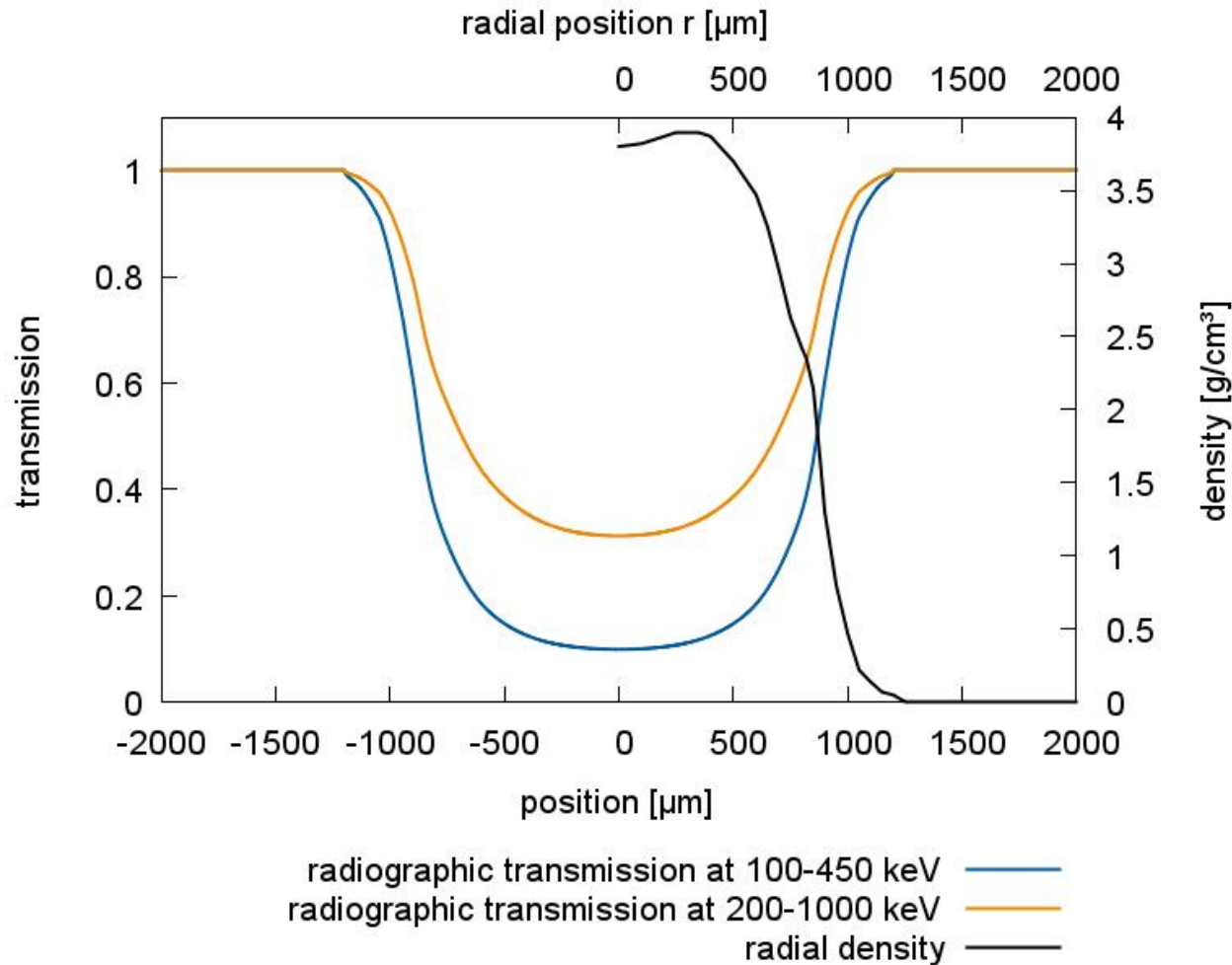
Experiment Simulation at 0.5x T
 Simulation with Ka only Simulation at 2x T
 Simulation at 1x T

Problems occur at higher T_0 due to steepness of T-gradients & 2D effects

X-Ray Radiography @ FAIR



X-Ray Radiography @ FAIR



Snapshot:
Expansion of a solid lead
cylinder $r = 300 \mu\text{m}$
close to critical point

$$I_{\text{max}} = 10^{19} \text{ W/cm}^2, E > 50 \text{ J}$$

→ $> 10^{12}$ bremsstrahlung-
photons ($4\pi \text{ sr}$)
in relevant spectral
range!

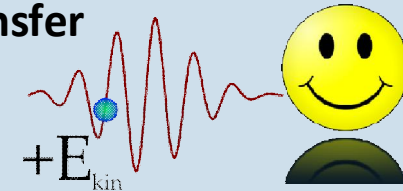
Density taken from N.A.Tahir et al., Phys. Rev. Lett. 95, 035001

Summary

- ✓ First laser pump-probe experiment at PHELIX
- ✓ Electron generation & transport:
 - Good agreement between simple model and full 3D hybrid PIC
 - 3D effects negligible
 - Collisional + ohmic heating main contributors
 - Full refluxing
- ✓ Wire Hydrodynamics:
 - Agreement (1D) at moderate temperatures
 - Good reproduction of „burning-speed“
 - Not-so-good agreement at high temperatures
 - 2D effect
- ✓ Smaller exp. errorbar → test of EOS ($\Delta = 10-20\%$)
- ✓ X-ray radiography: promising complementary method to probe dense, heavy ion produced plasmas

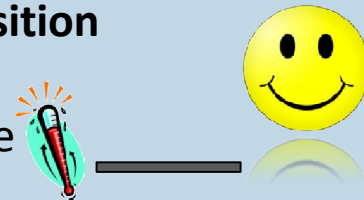
Energy transfer

Laser → e⁻



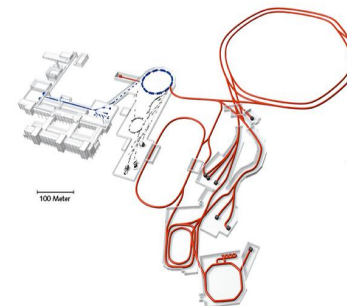
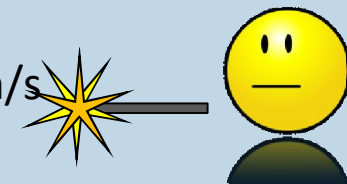
Energy deposition

inside the
target volume



Expansion

($v \approx v_s \sim 30 \text{ km/s}$
 $= 30 \mu\text{m/ns}$)



Thanks are given to the collaborators...

B. Aurand^{1,4}, M. Basko^{1,8}, B. Ecker^{4,6}, T. Kühl^{2,4}, T. Ma⁷,
F. Rosmej⁵, B. Zielbauer^{2,6}, D. Zimmer² and P. Neumayer^{1,3}

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⁴University of Mainz, Mainz; ⁵UPMC, Paris, France; ⁶HIJ, Jena;

⁷LLNL, Livermore, USA; ⁸ITEP, Moscow, Russia

I would like to thank the PHELIX team for its support.

Thank YOU for your attention.