

Riezlern 2010

Beam Dynamics and Emittance Growth

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Motivation

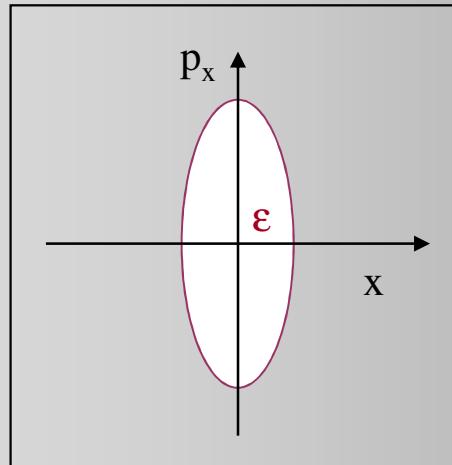
Requirements on Accelerator physics
- Luminosity

$$L = \frac{\dot{N}}{\sigma_s}$$

Current density at
„Final Focus“

$$J = \frac{1}{A} \cdot \dot{N}$$

Beam emittance



minimum spot size

Beam current I_s

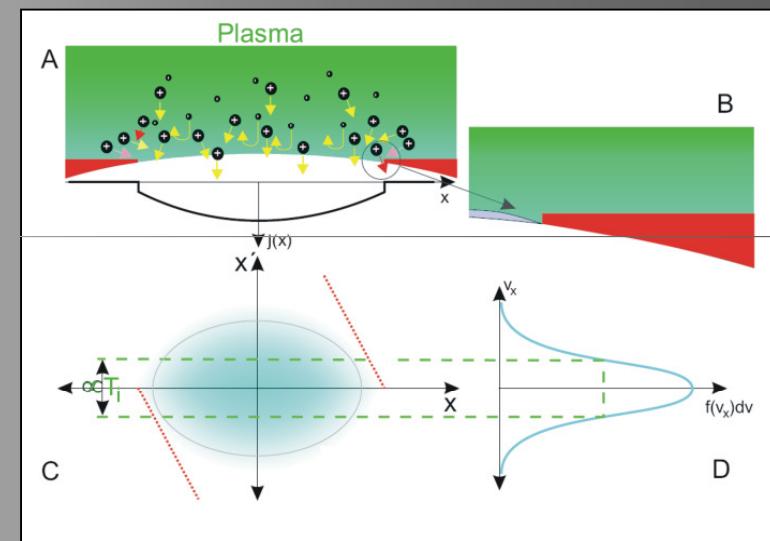
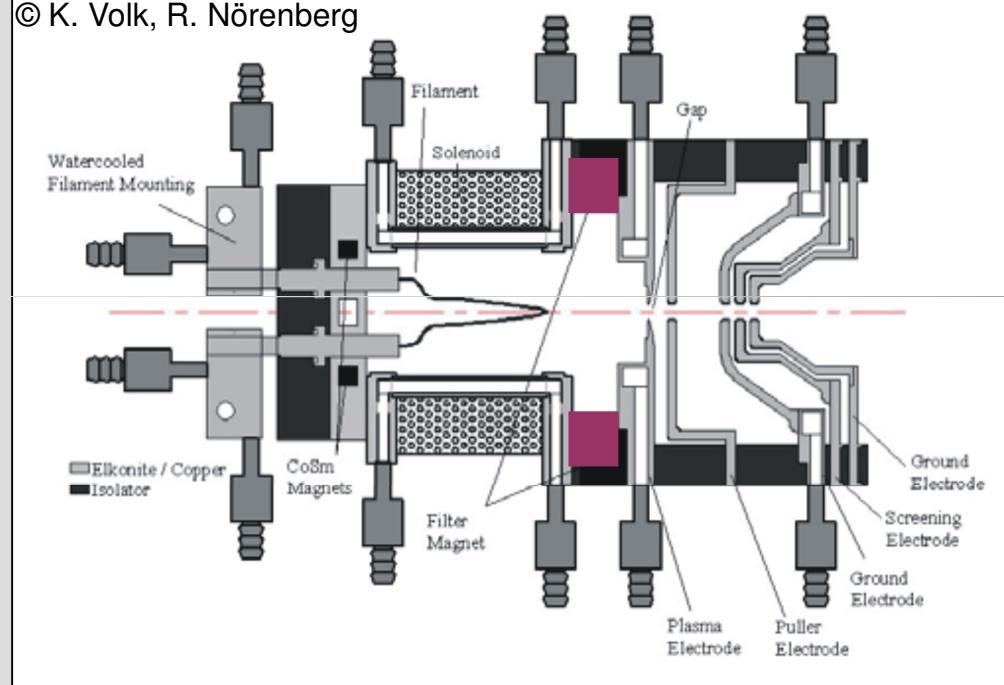
$$r_{\min} = \frac{\epsilon_\perp}{p_\perp}$$

Space Charge !

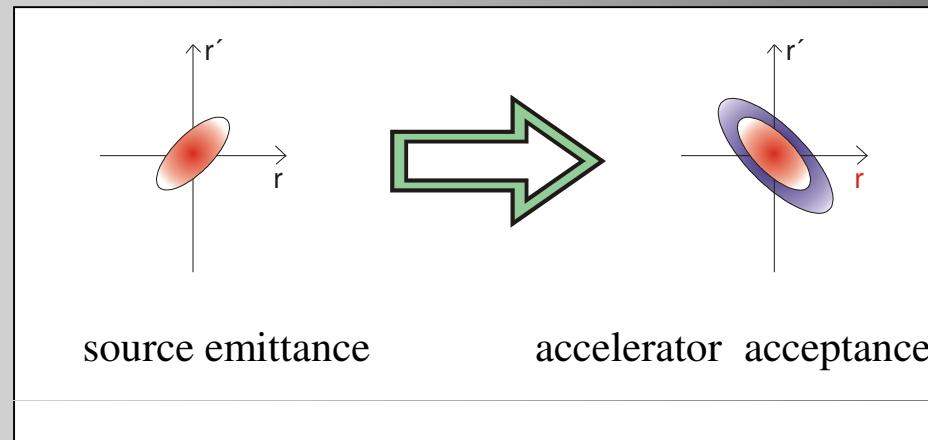
Beam emittance vs. Beam current

Beam Extraction

© K. Volk, R. Nörenberg



Beam Transport



small emittance:

- low T_i (laminar beam)
- distribution function

Assumptions:

- transverse plane
- coasting beam
- no external field
- decompensated

Emittance growth:

- external fields (lens aberration)
- collisionless relaxation
- compensation process

Non Linear Field Energy

$$\epsilon_{x,rms} = \sqrt{\langle x^2 \rangle \langle x'^2 \rangle - \langle xx' \rangle^2}$$

Sacherer

$$\frac{d}{dz} \langle \epsilon_{x,rms} \rangle^2 = 2 \frac{q}{Amv_i^2} \left(\langle x^2 \rangle \langle x'E_x \rangle - \langle xx' \rangle \langle xE_x \rangle \right)$$

Th. Weis

$$\langle x'E_x \rangle = \frac{1}{Nqv_i} \iint E_x j_x dx dy$$

Wangler

$$\iint E j dx dy = -v_i \frac{d}{dz} W$$

$$\boxed{\langle x'E_x \rangle \sim \frac{d}{dz} W}$$

$$\frac{1}{\langle x^2 \rangle} \frac{d \langle x^2 \rangle}{dz} \langle xE_x \rangle + \frac{1}{\langle y^2 \rangle} \frac{d \langle y^2 \rangle}{dz} \langle yE_y \rangle = -\frac{2}{Nq} \frac{d}{dz} W_h$$

Anderson

Non Linear Field Energy

$$\frac{1}{\langle x^2 \rangle} \frac{d}{dz} \langle \epsilon_{rms,x}^2 \rangle + \frac{1}{\langle y^2 \rangle} \frac{d}{dz} \langle \epsilon_{rms,y}^2 \rangle = -\frac{2}{Amv_i^2 N} \frac{d}{dz} (W - W_h)$$

relaxation time



$$\frac{d}{dz} \epsilon_{rms,x}^2 = -\frac{1}{8} \langle x^2 \rangle K \frac{d}{dz} W_{nl}$$

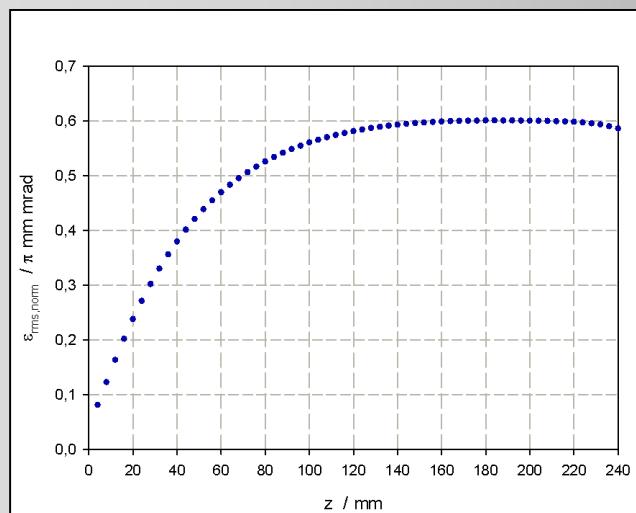
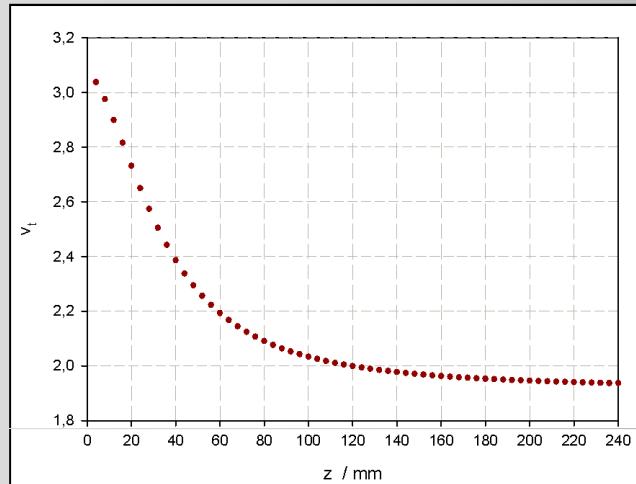
ion distribution

$$\lambda_p = \frac{\omega_p}{2\pi v_i}$$

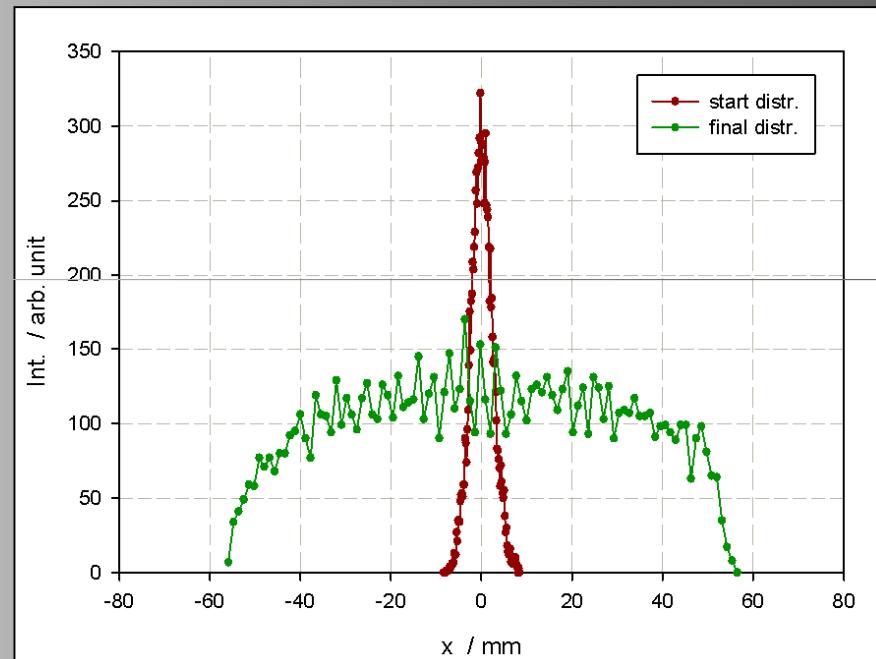
$$\Delta \epsilon_{rms,x} = \sqrt{\epsilon_{rms,x,final}^2 - \epsilon_{rms,x,start}^2} = \sqrt{\frac{\langle x^2 \rangle K \Delta W_{nl}}{8}}$$

$$v_t = \frac{\bar{x}^4}{x^2}$$

Thermalisation

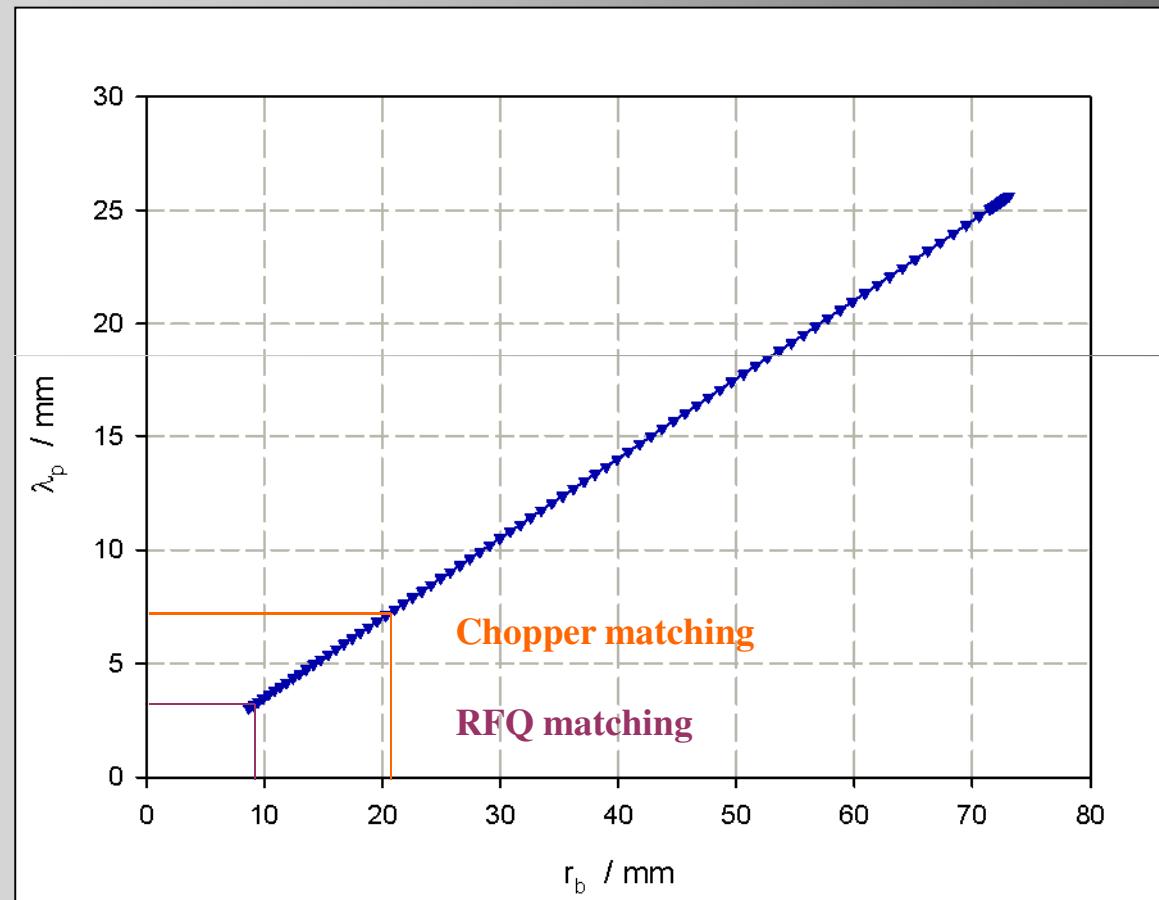


Example I: Gaussian start distribution

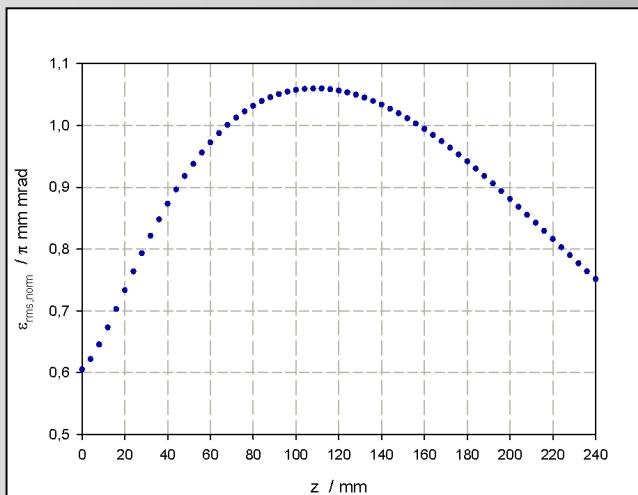
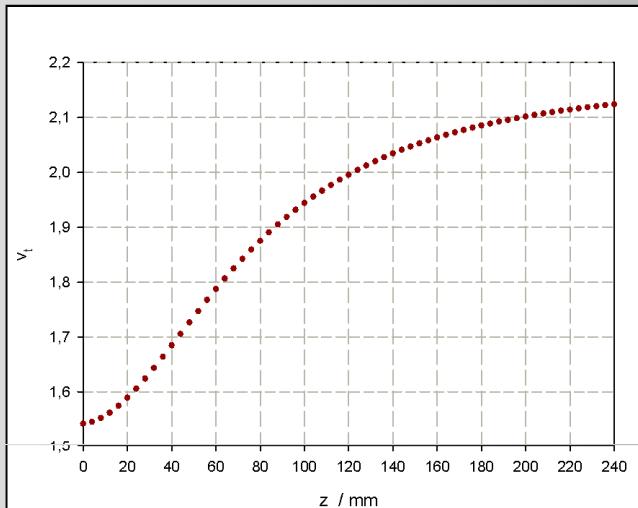


$$\Delta\epsilon_{rms,x} = 8 !$$

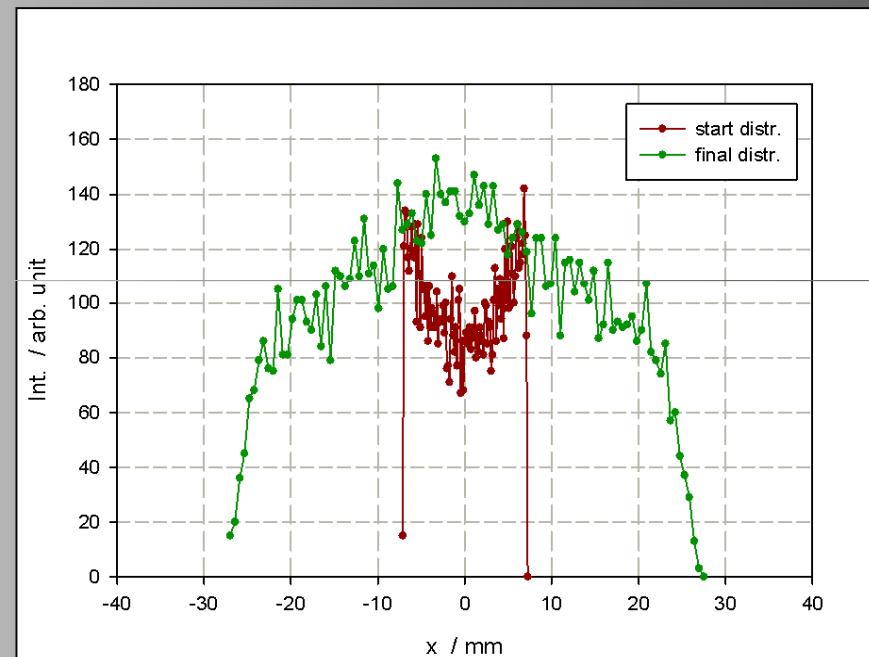
Relaxation Time



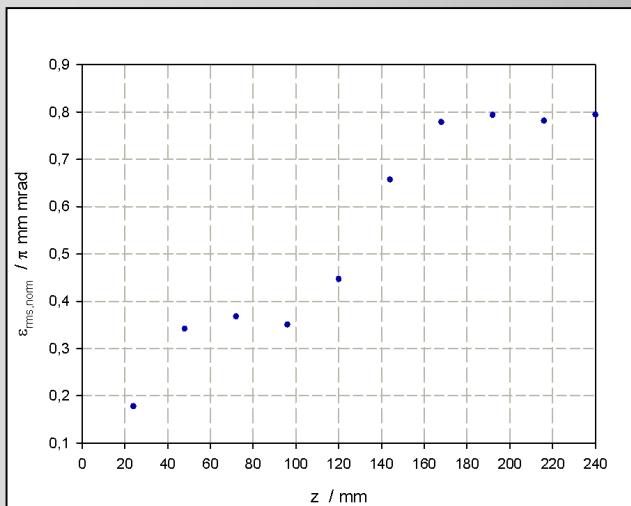
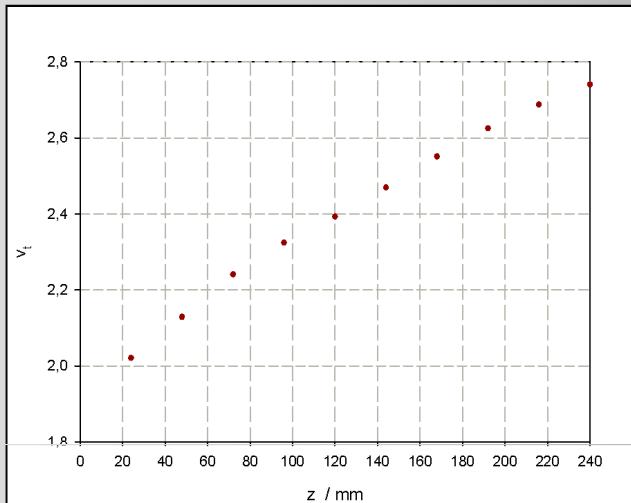
Thermalisation



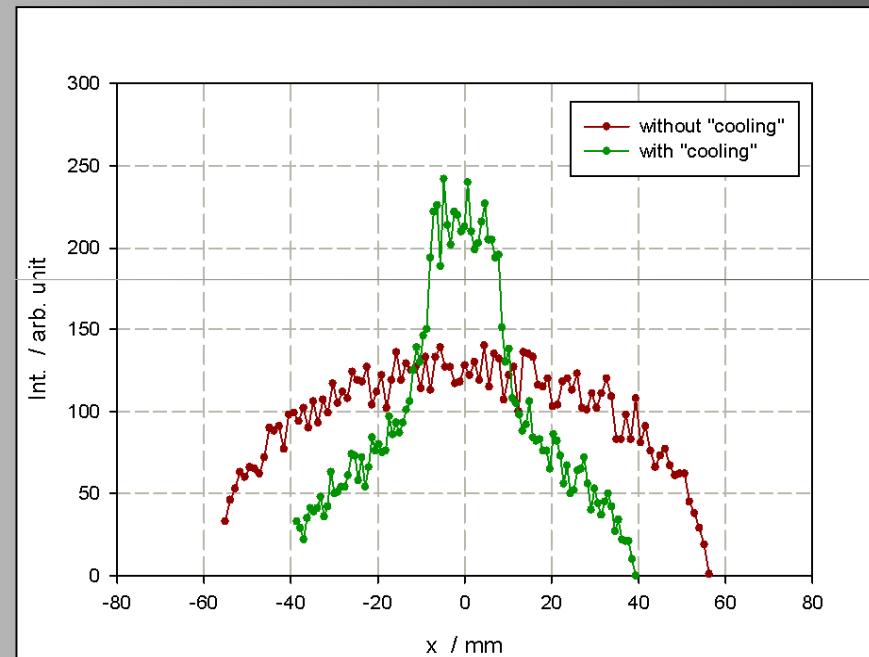
Example II: hollow beam



Thermalisation

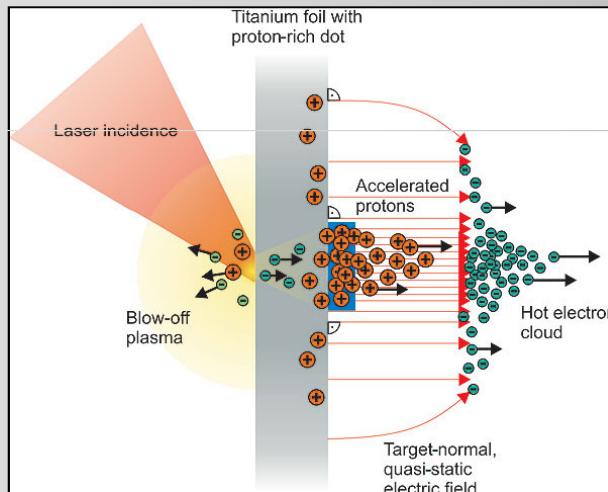


Example III: electron beam „cooling“

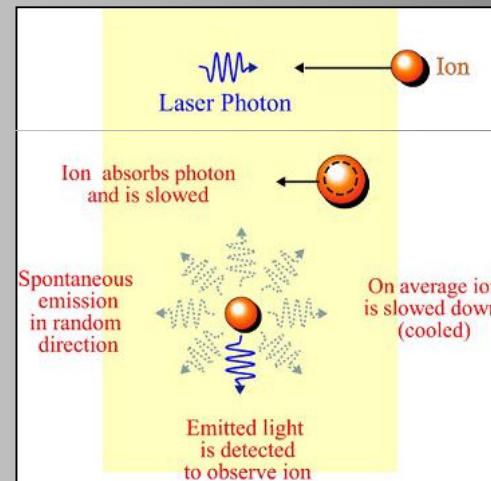


Cold Ion Beams

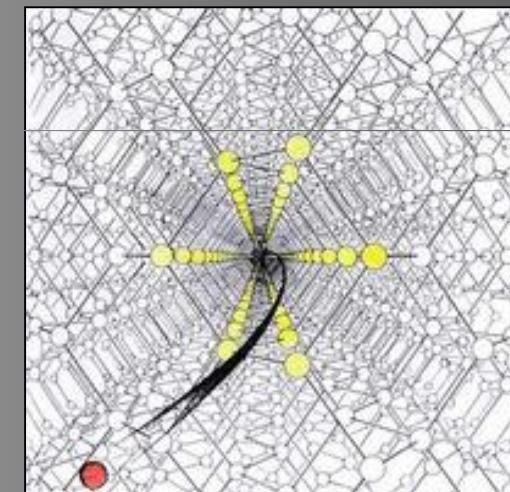
production of cold ion beams



LASER cooling



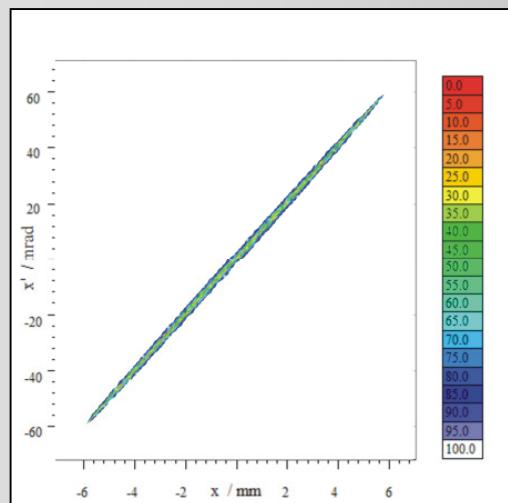
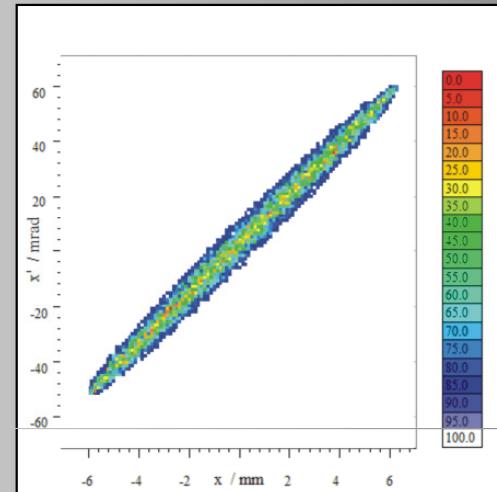
channeling



Reduction and Growth of Beam Emittance

Cooling

Compression



heating

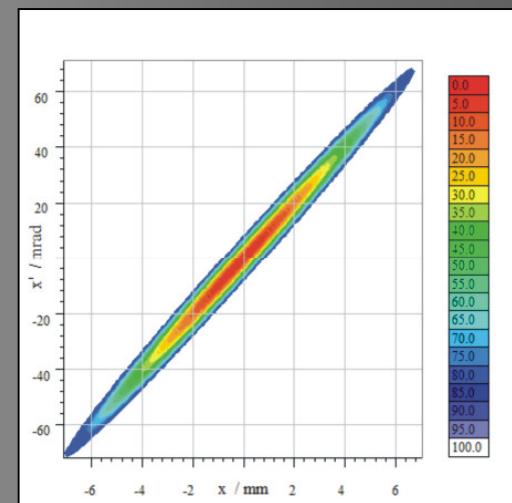
collisionless
relaxation

$$\tau_r = \frac{4.8 \cdot 10^{-14} \cdot n_i \cdot \ln \Lambda}{T_i^{3/2}}$$

$$\tau_p = \frac{2\pi}{\omega_p}$$

1.78 ms

166 ns



Thank You!

Requirements on Accelerator physics
- Luminosity -

$$L = \frac{\dot{N}}{\sigma_s}$$